



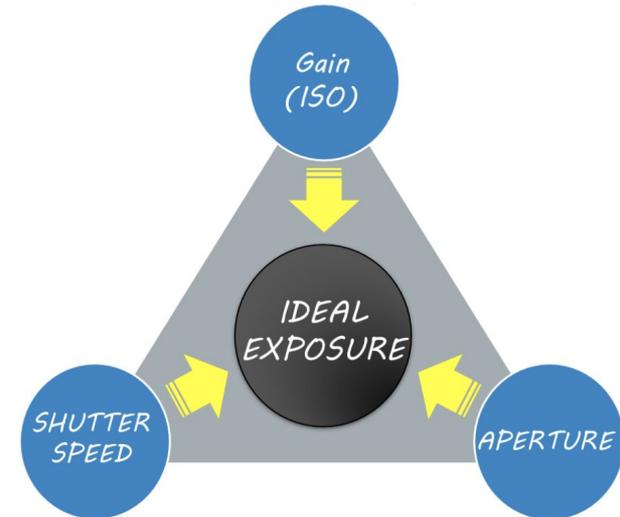
# Semillero de Investigación “Hands - on” Computer Vision

A Sony 7K 616 camera is shown from a front-three-quarter view. The camera is black and has a lens attached. The lens shows a sunset scene with a bright orange sun partially obscured by a dark horizon. The text 'SESIÓN 2: DE FOTONES A PÍXELES' is overlaid in large, white, bold, sans-serif font across the center of the image. The camera's body has 'SONY' on the top, '7K 616' on the right side, and 'MULTIFOCUS' on the left side. The lens has 'SONY' and 'G OLYMPUS' visible on its barrel. The camera is resting on a surface of small, dark, pebbly stones.

**SESIÓN 2:  
DE FOTONES A  
PÍXELES**

# Contenidos

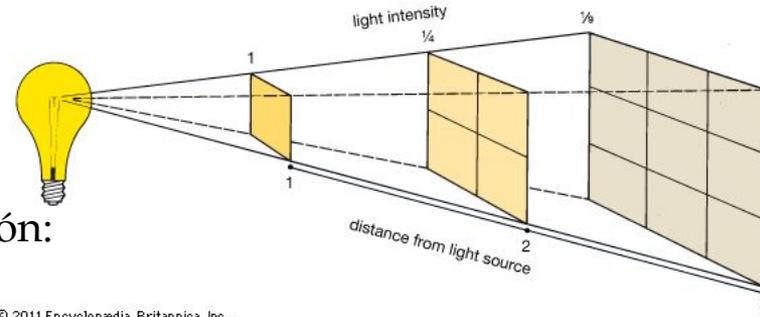
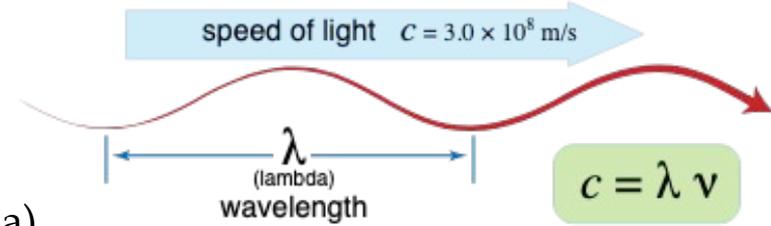
1. La cámara oscura (pinhole camera)
2. Formación de imágenes (FOV, AOV, DoF)
3. Triángulo de la exposición
4. Pipeline de procesamiento de imágenes
5. Transformaciones de imágenes



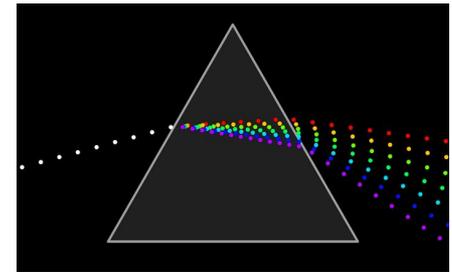
# **1. Cámara oscura**

# La luz

1. La luz viaja **muy rápido** ( $c = 300.000 \text{ km/s}$ )
2. La luz tiene una **doble naturaleza** (onda y/o partícula)
3. Viaja en **línea recta** (menor distancia, parsimonia)
4. Varía en **intensidad** (inverse square law)
5. **Interactúa** con la materia (cambia velocidad y dirección: **reflexión, refracción, absorción, difracción**, etc.)
6. Tiene muchos **colores** (dispersión)
7. Contiene **energía e información** (radio, celulares, fibra óptica, etc.)

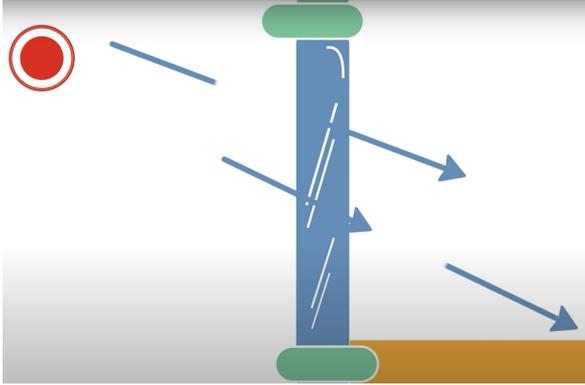


© 2011 Encyclopædia Britannica, Inc.

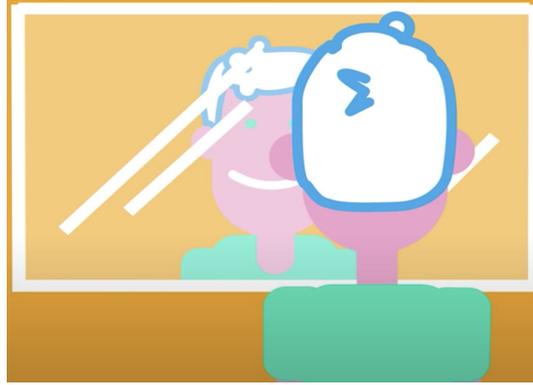


# Propagación de la luz

Transmisión



Reflexión



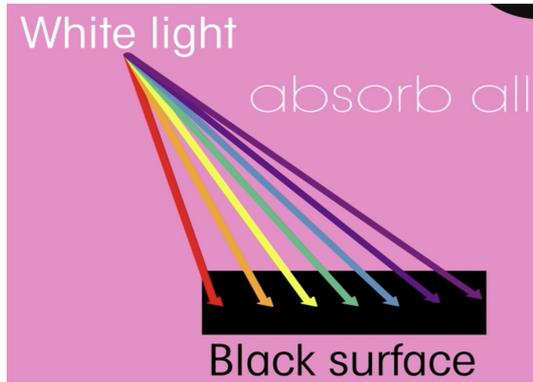
Refracción



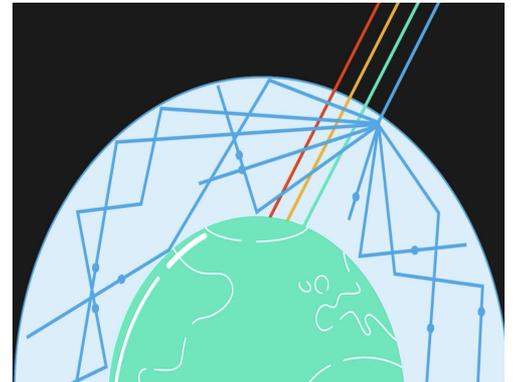
Difracción



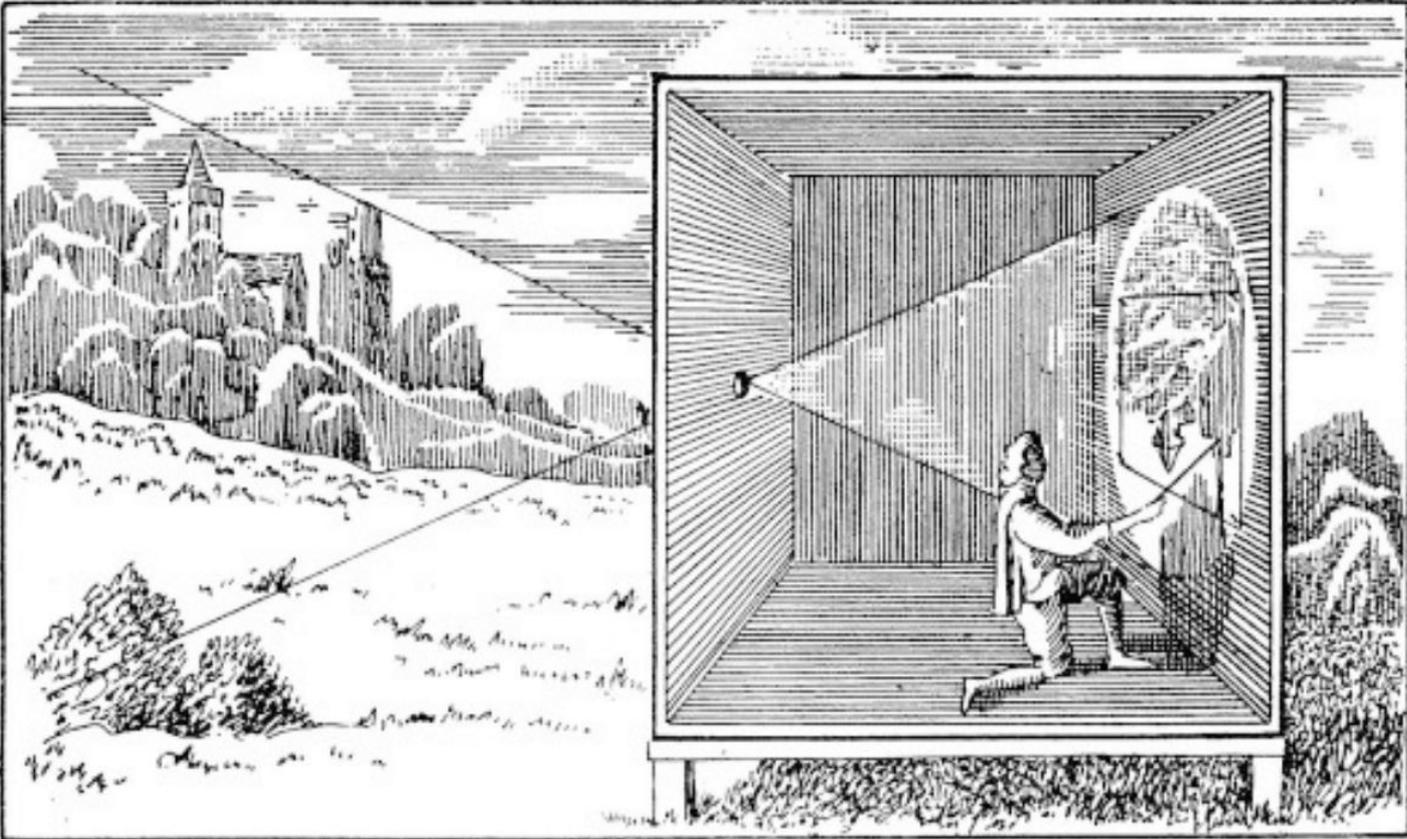
Absorción



Scattering



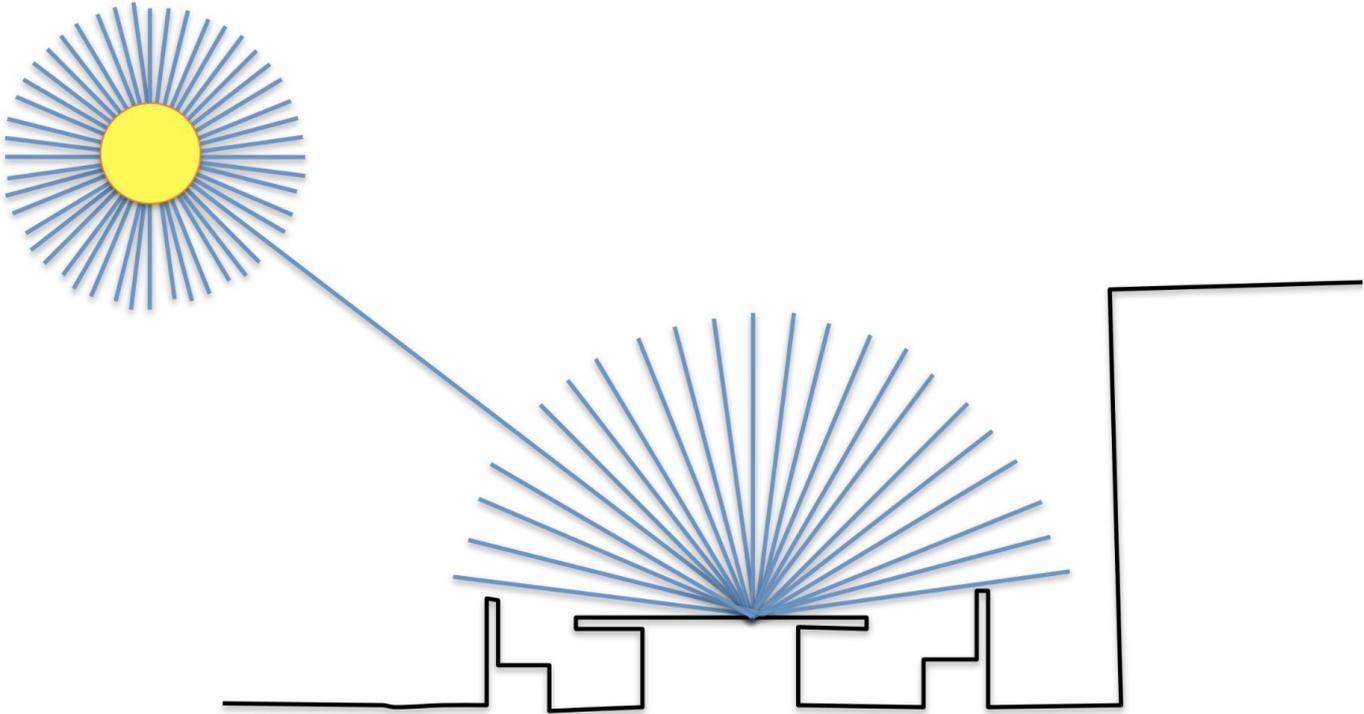
# Pinhole Camera / Camera Obscura



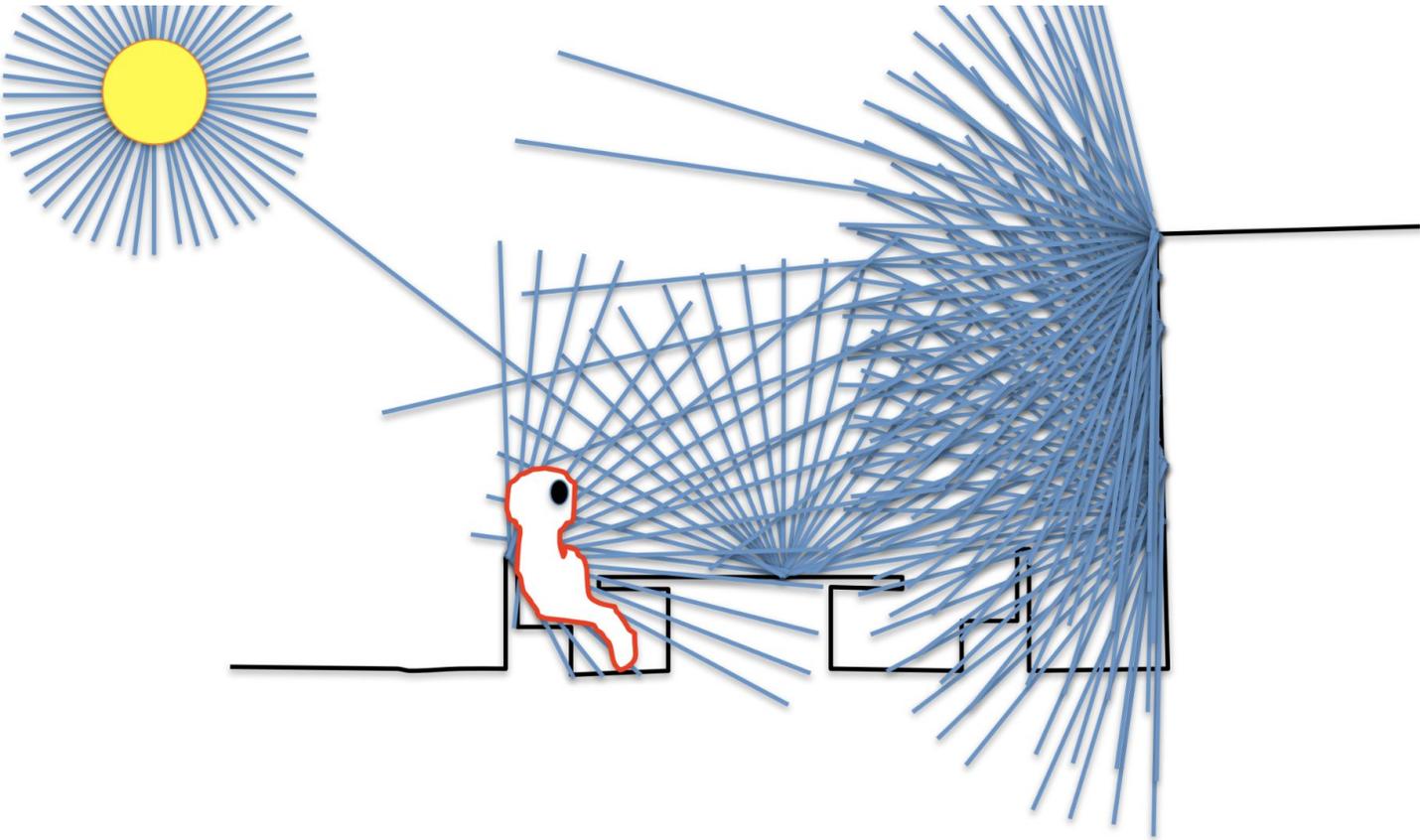
Mo-Ti (Chinese Philosopher) 470-390 BC

# Demo: Camera obscura

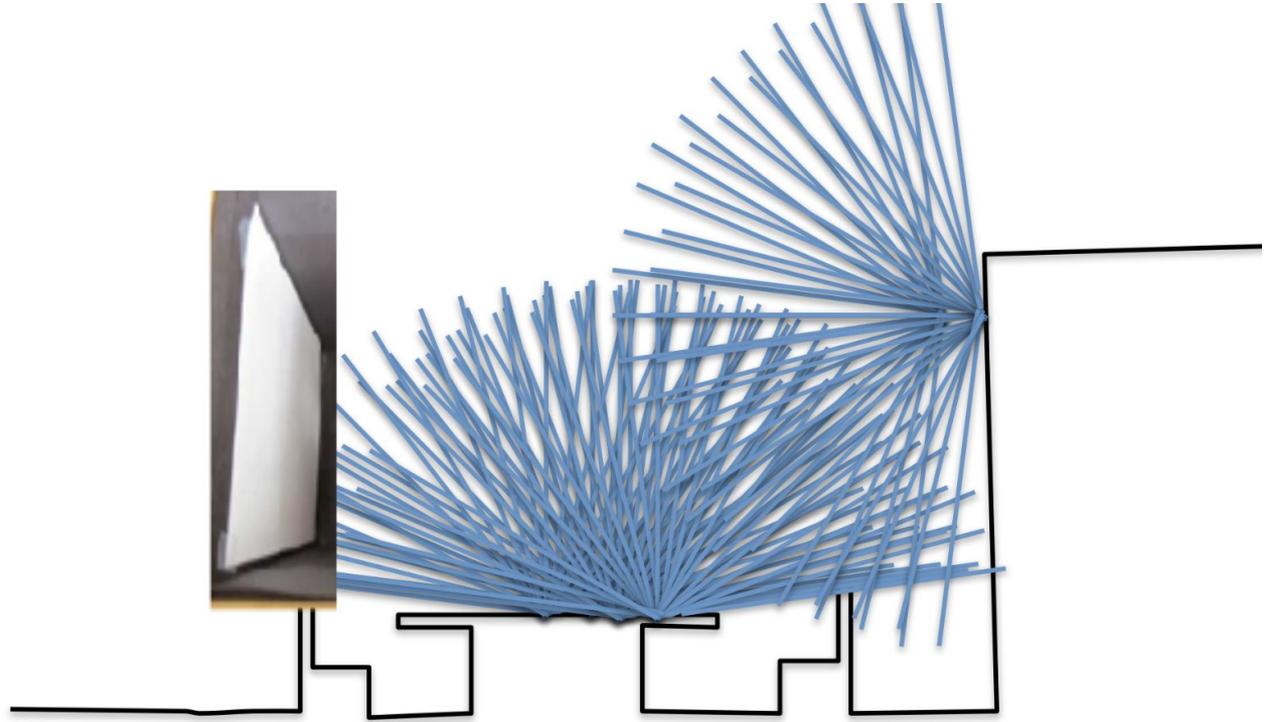
# Propagación de la luz



# Propagación de la luz



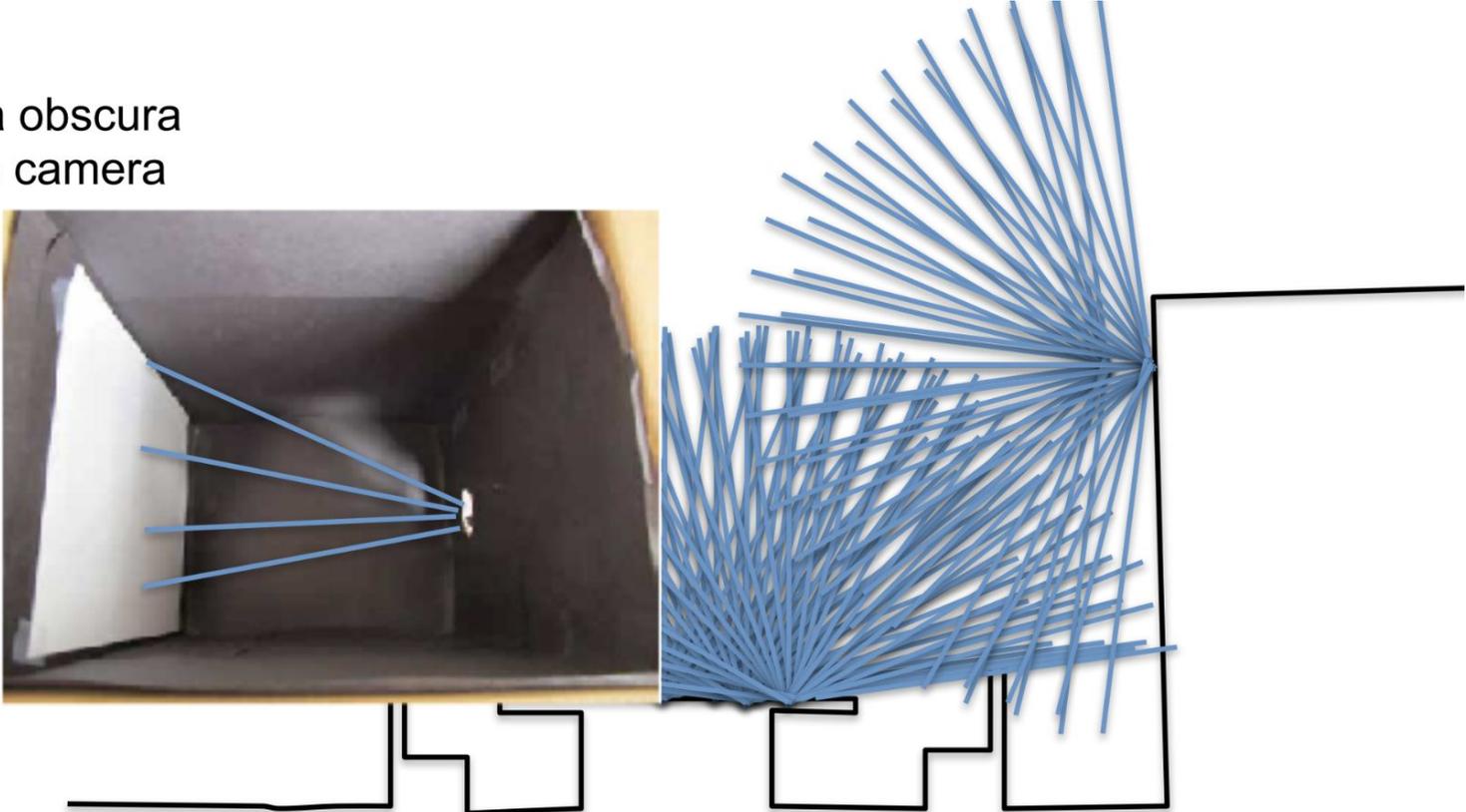
# Propagación de la luz

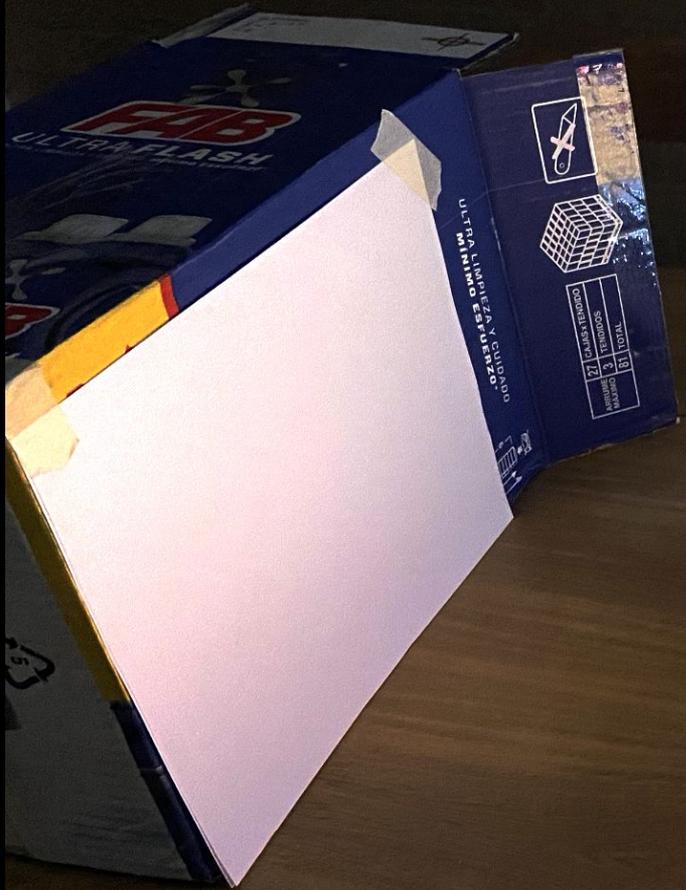


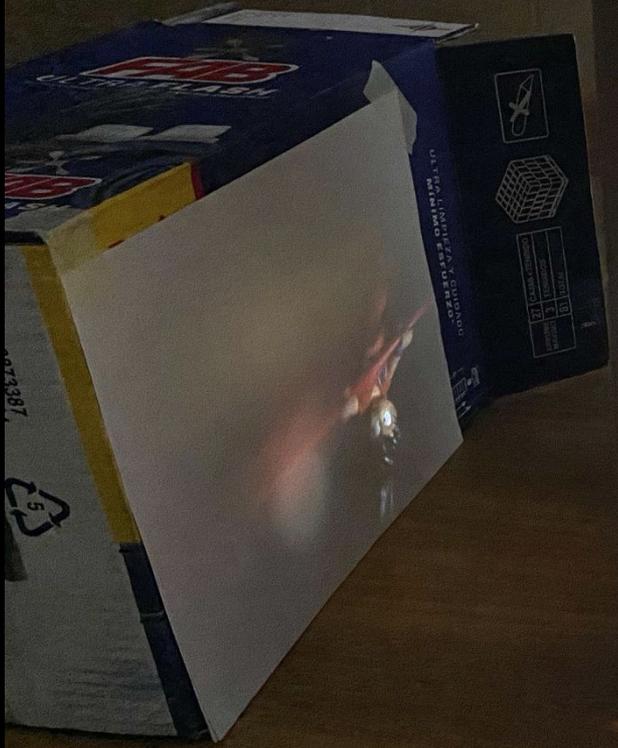
Why is there no picture appearing on the paper?

# Propagación de la luz

The camera obscura  
The pinhole camera

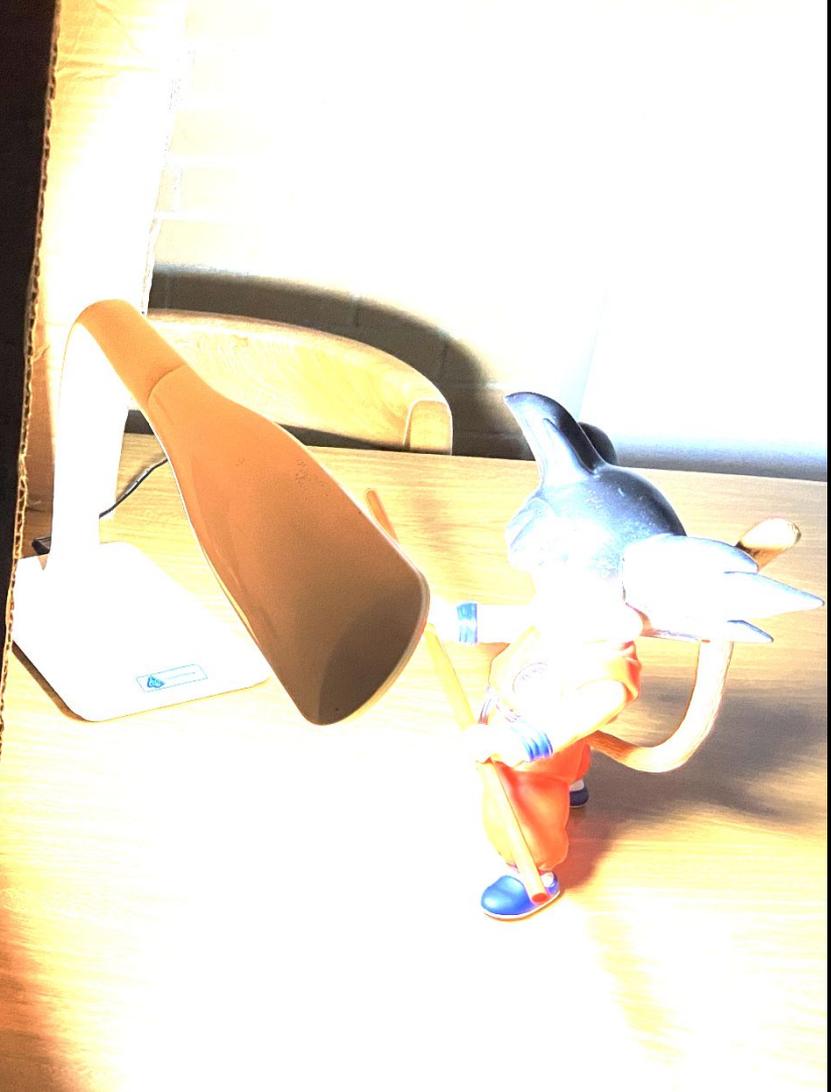






42460001

PAVCO PAVCO PAVCO PAVCO PAVCO PAVCO PAVCO



# Construyendo la Camera Obscura





## **2. Formación de imágenes**

# Fotografía analógica



Óptica para enfocar  
la luz en un plano  
de imagen



Película para capturar  
luz enfocada  
(proceso químico)

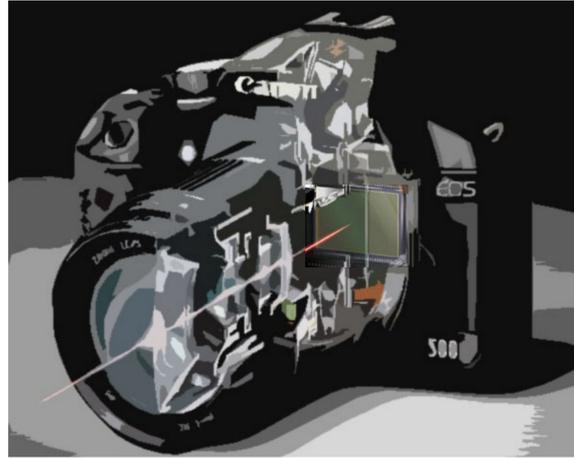


Cuarto oscuro para  
posprocesamiento limitado  
(proceso químico)

# Fotografía digital



Óptica para enfocar  
la luz en un plano  
de imagen

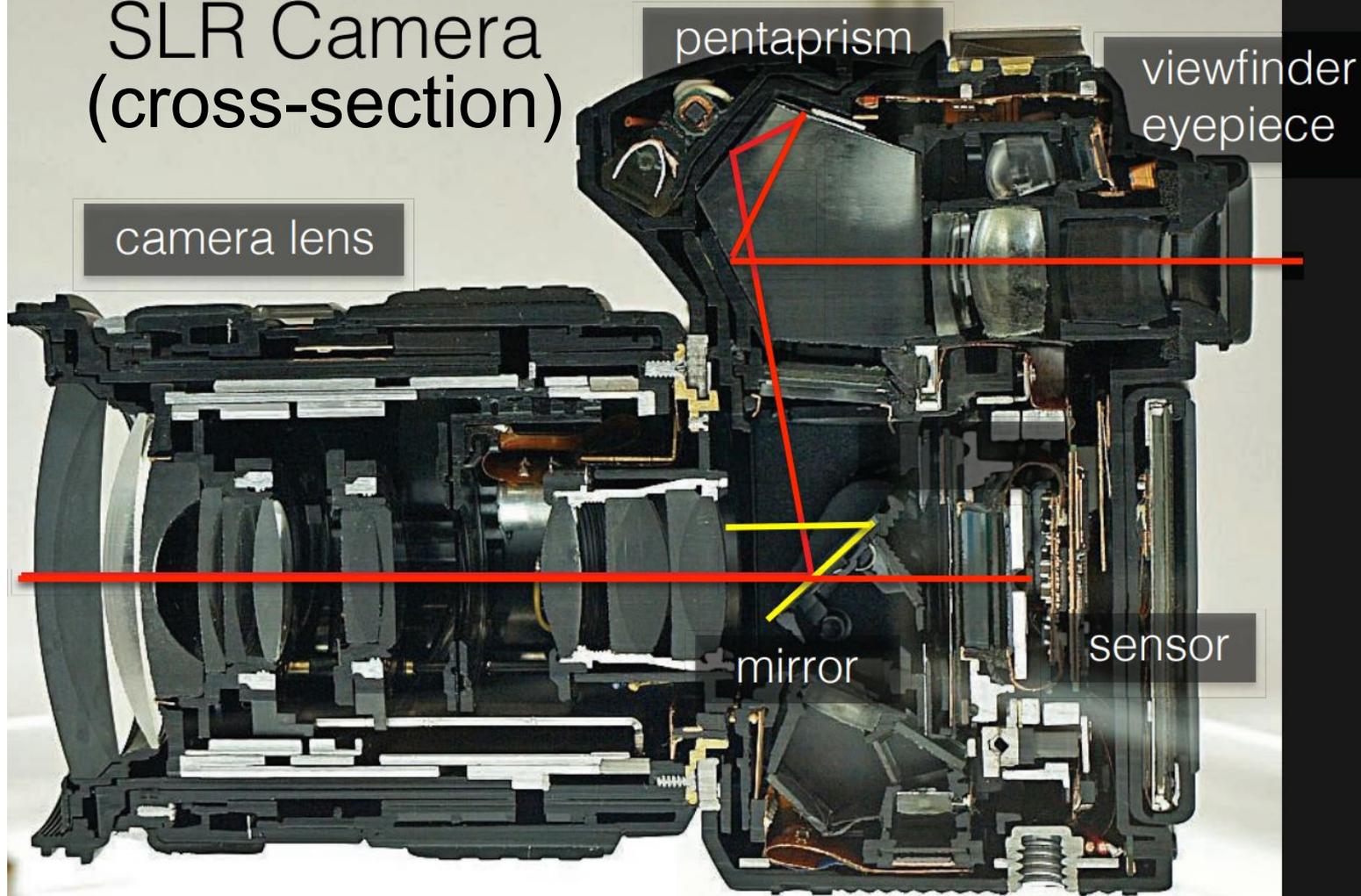


Sensor digital para  
capturar luz enfocada  
(proceso eléctrico)



Procesador integrado para  
posprocesamiento  
(proceso digital)

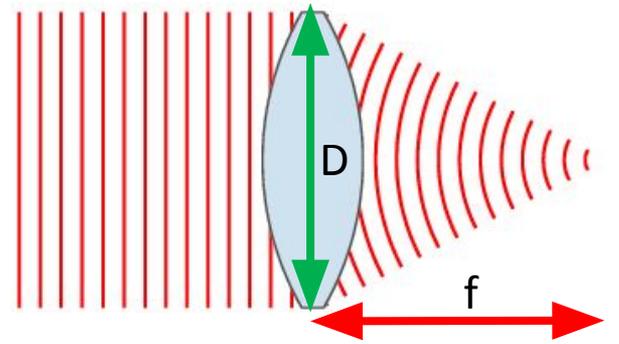
# SLR Camera (cross-section)



# Conceptos básicos de lentes

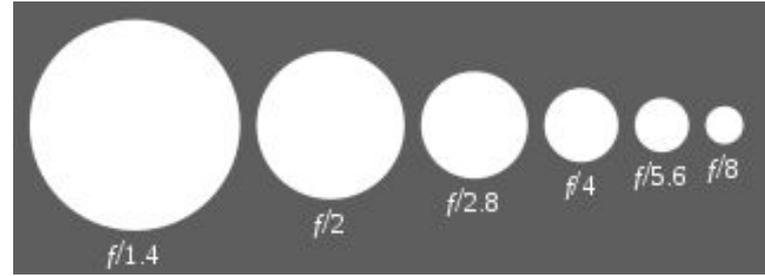
## 1. Propiedades de los lentes (F/#, power)

- Distancia focal
- Apertura (D)
- F-number (f/#):  $f/D$
- Power (dioptría) =  $1/f$



## 2. Trazado de rayos básico (3 rayos son suficientes)

<https://ophysics.com/l12.html>

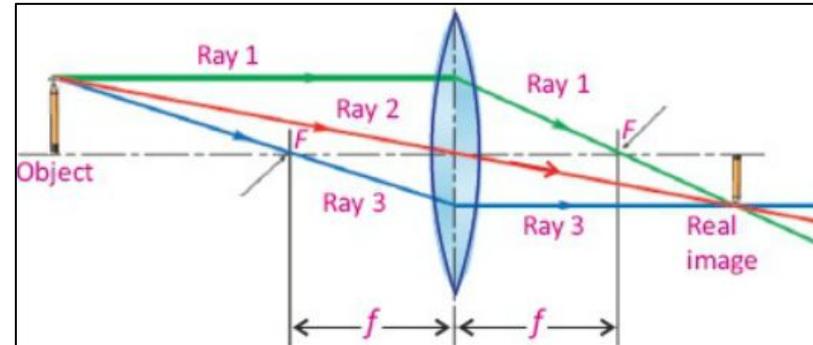


## 3. Trazado de rayos (Lens' Maker formula)

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$y_i = \frac{d_i \cdot y_o}{d_o}$$

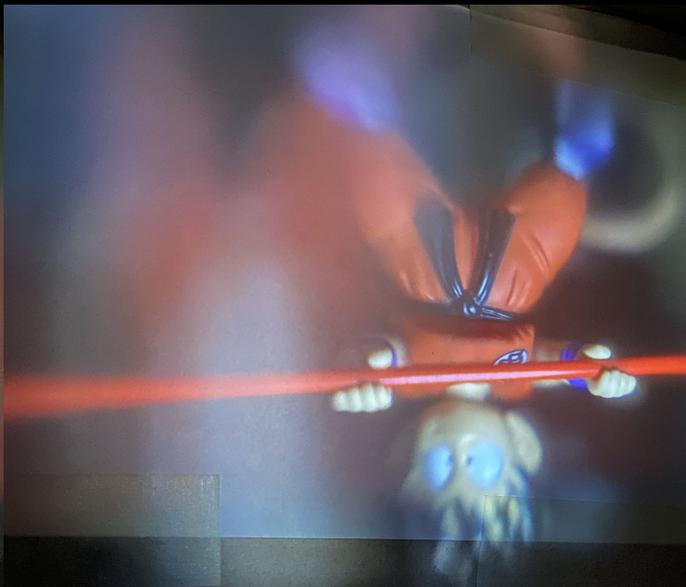
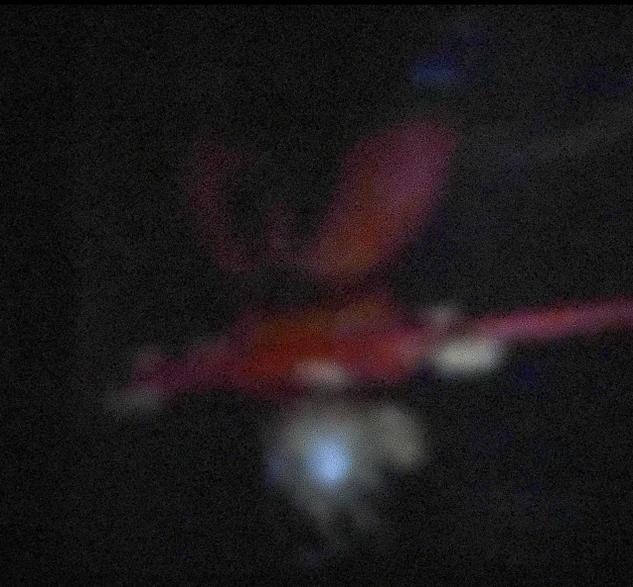
$$M = \frac{d_i}{d_o} = \frac{y_i}{y_o}$$



# Demo: Pinhole vs Lente





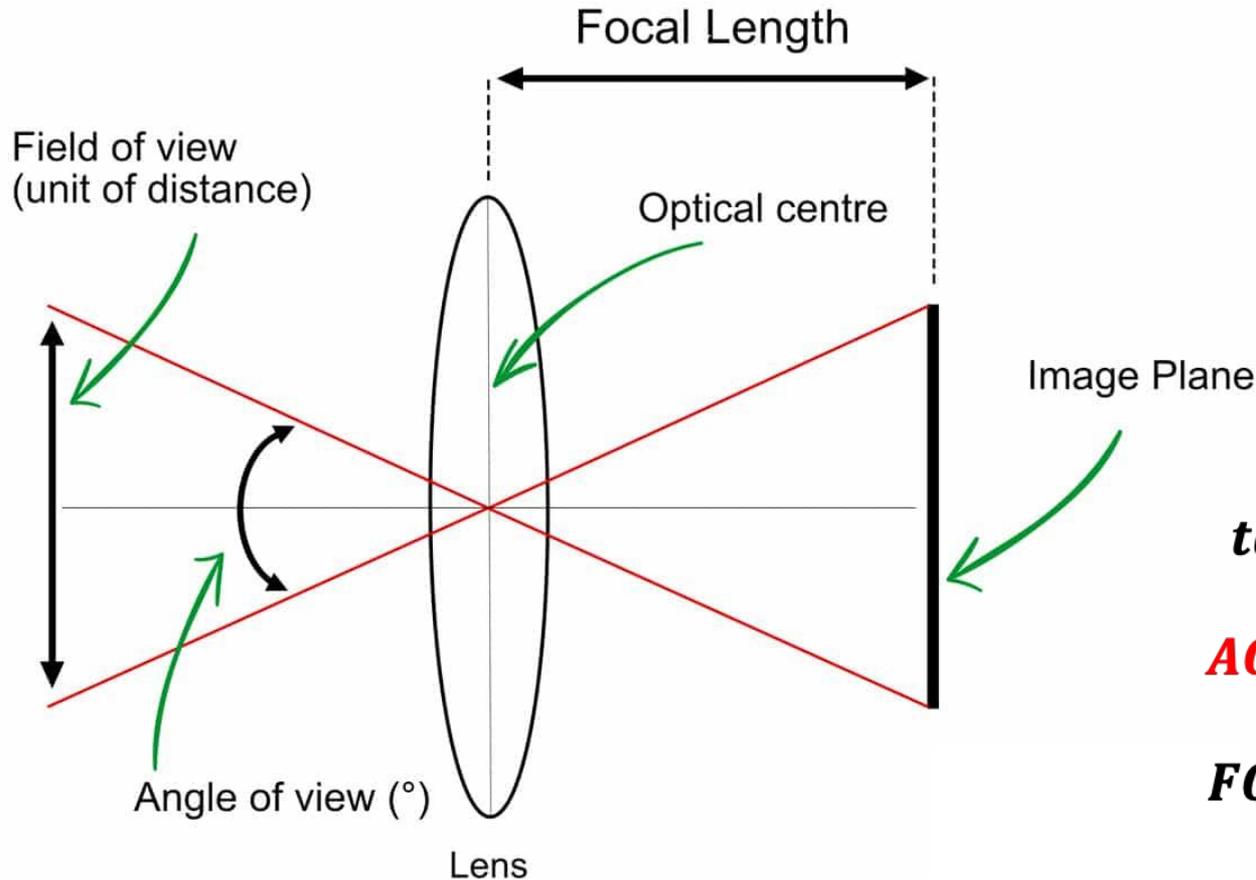




ULTRA LIMPIEZA Y CUIDADO  
MINIMO ESFUERZO\*



# Angle of view (AOV) vs. Field of View (FOV)



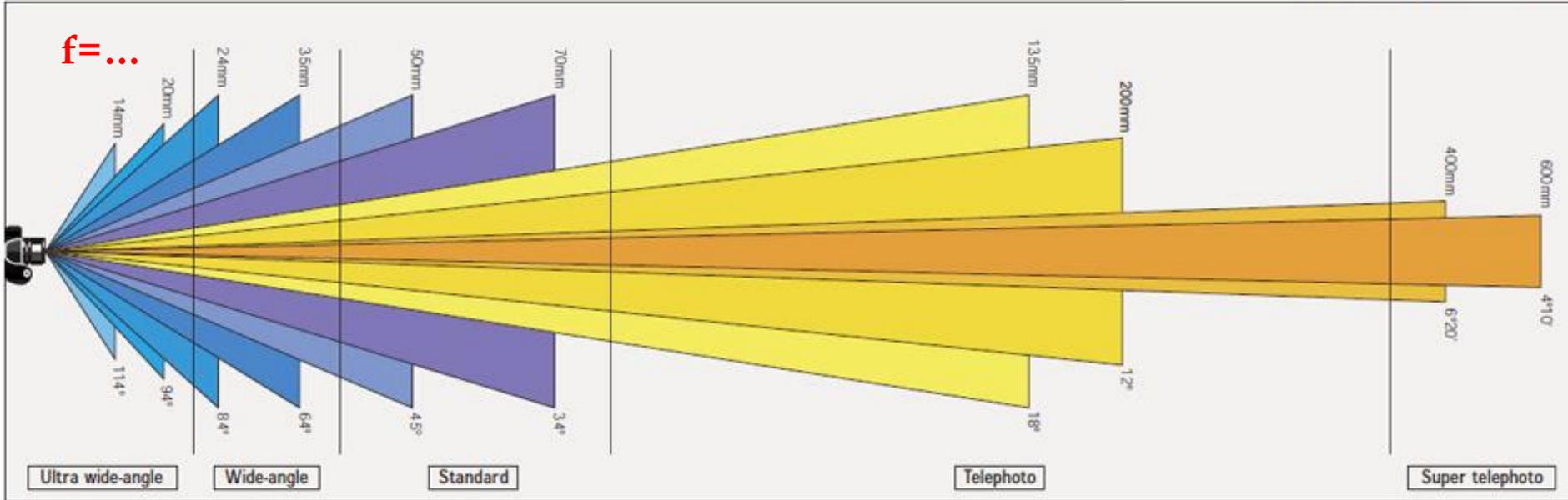
$$\tan\left(\frac{\alpha}{2}\right) = \frac{h/2}{f}$$

$$\mathbf{AOV} = \alpha = \mathbf{2\arctan\left(\frac{h}{2f}\right)}$$

$$\mathbf{FOV} = \mathbf{2\tan\left(\frac{AOV}{2} * d_o\right)}$$

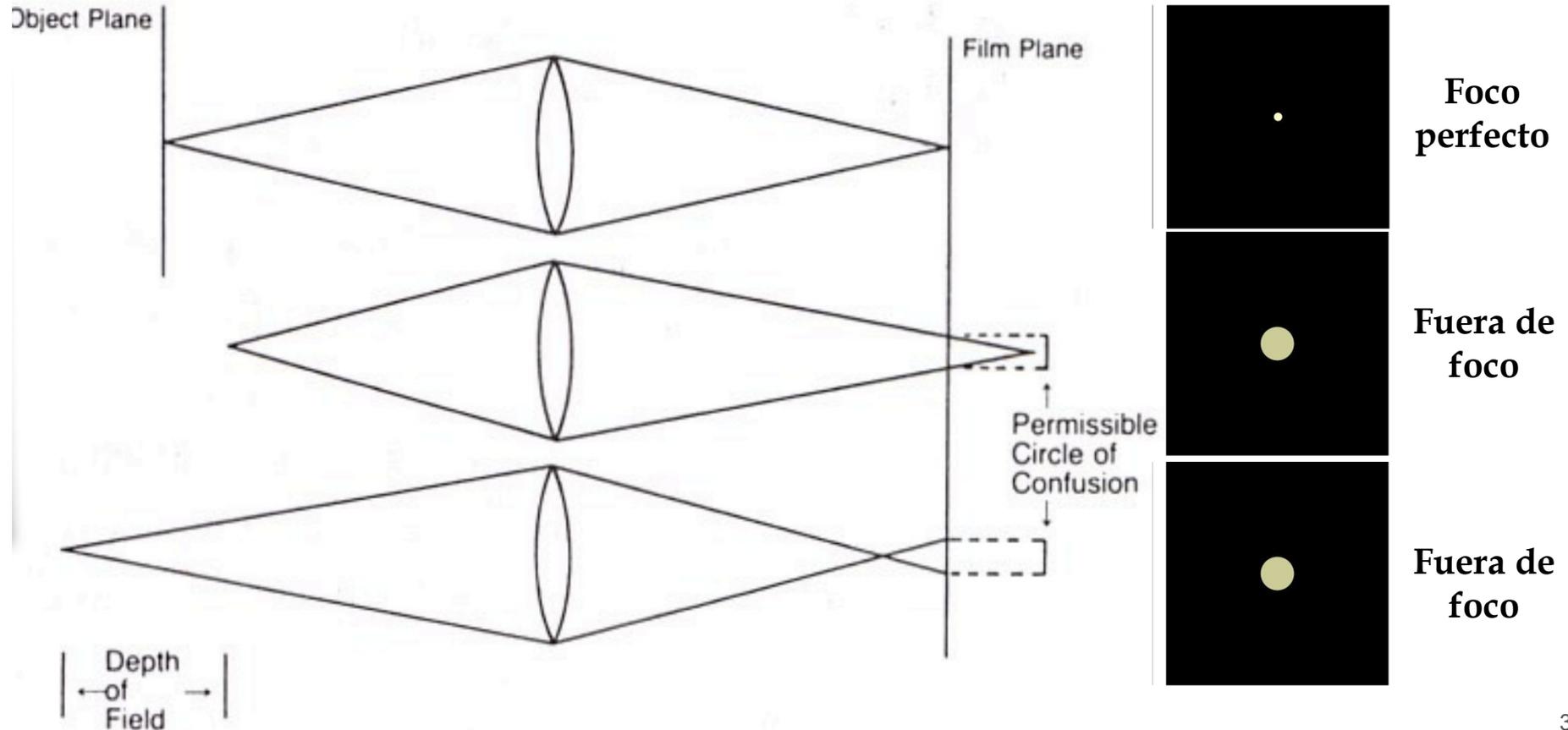
# Ejemplos de diferentes FOV

DIY w. h = 43 mm



Normal view seen by the human eye

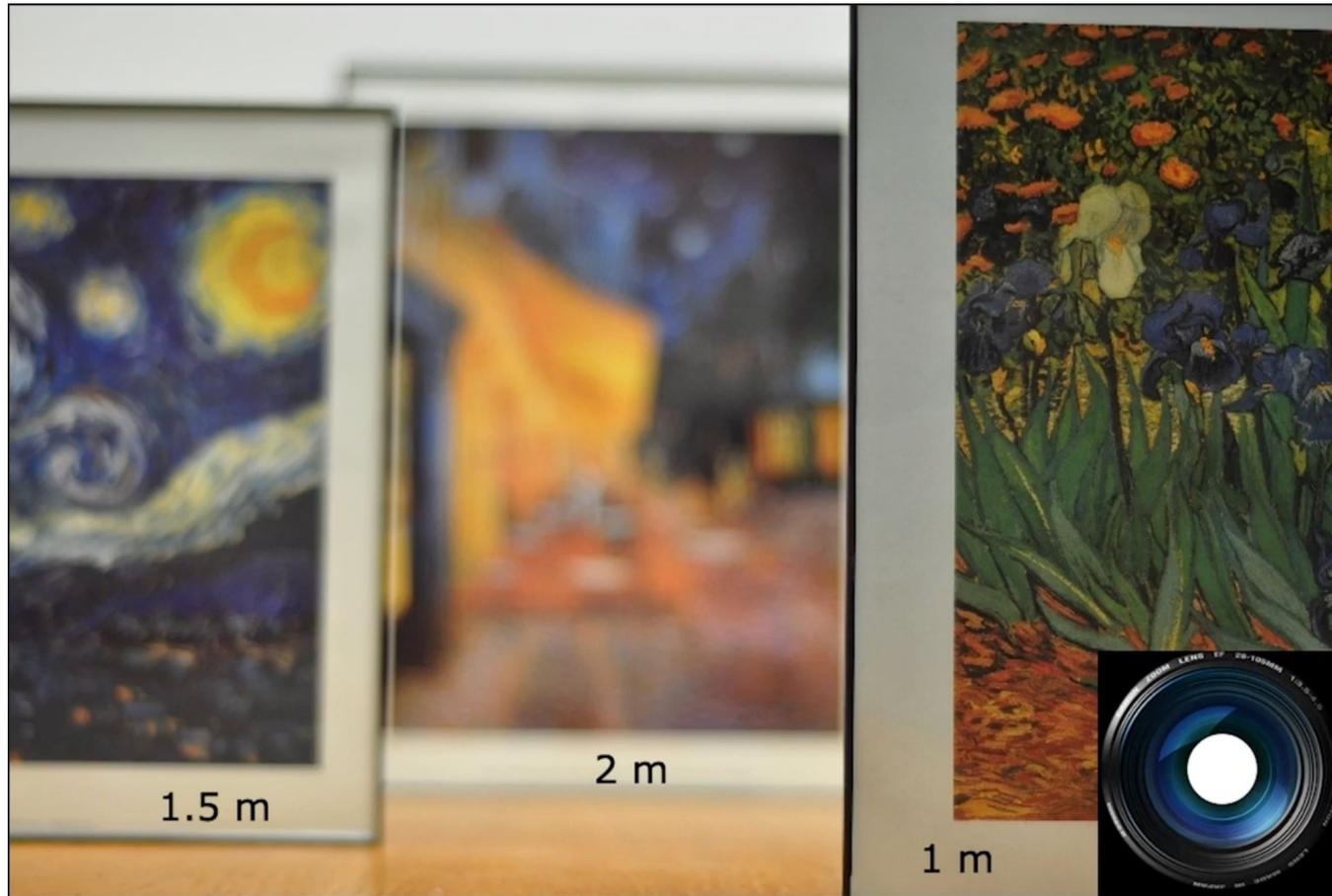
# Profundidad de campo (Círculo de confusión)



# Profundidad de campo (Depth of field, DoF)



# Example (Reducing aperture)



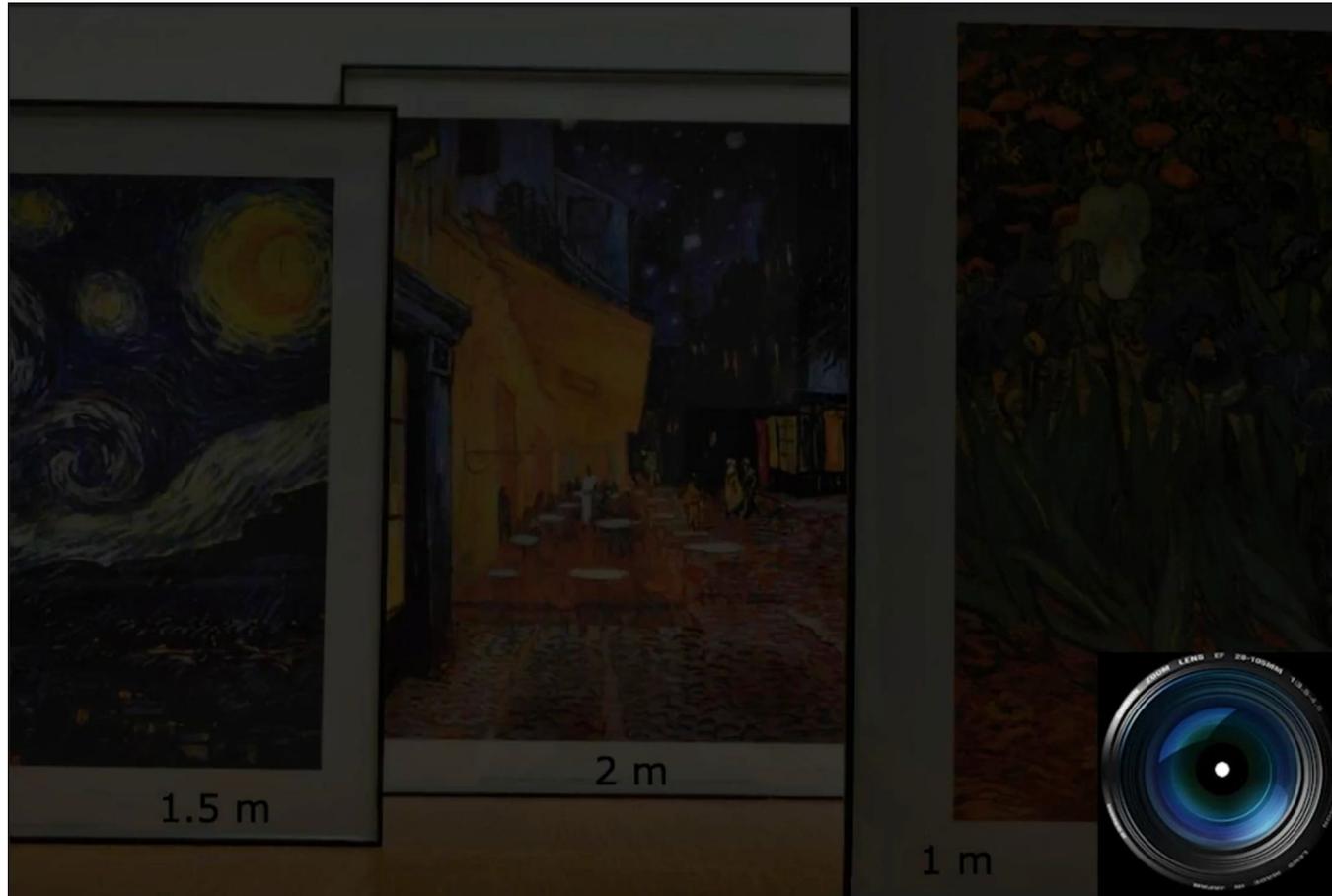
# Example (Reducing aperture)



# Example (Reducing aperture)



# Example (Reducing aperture)

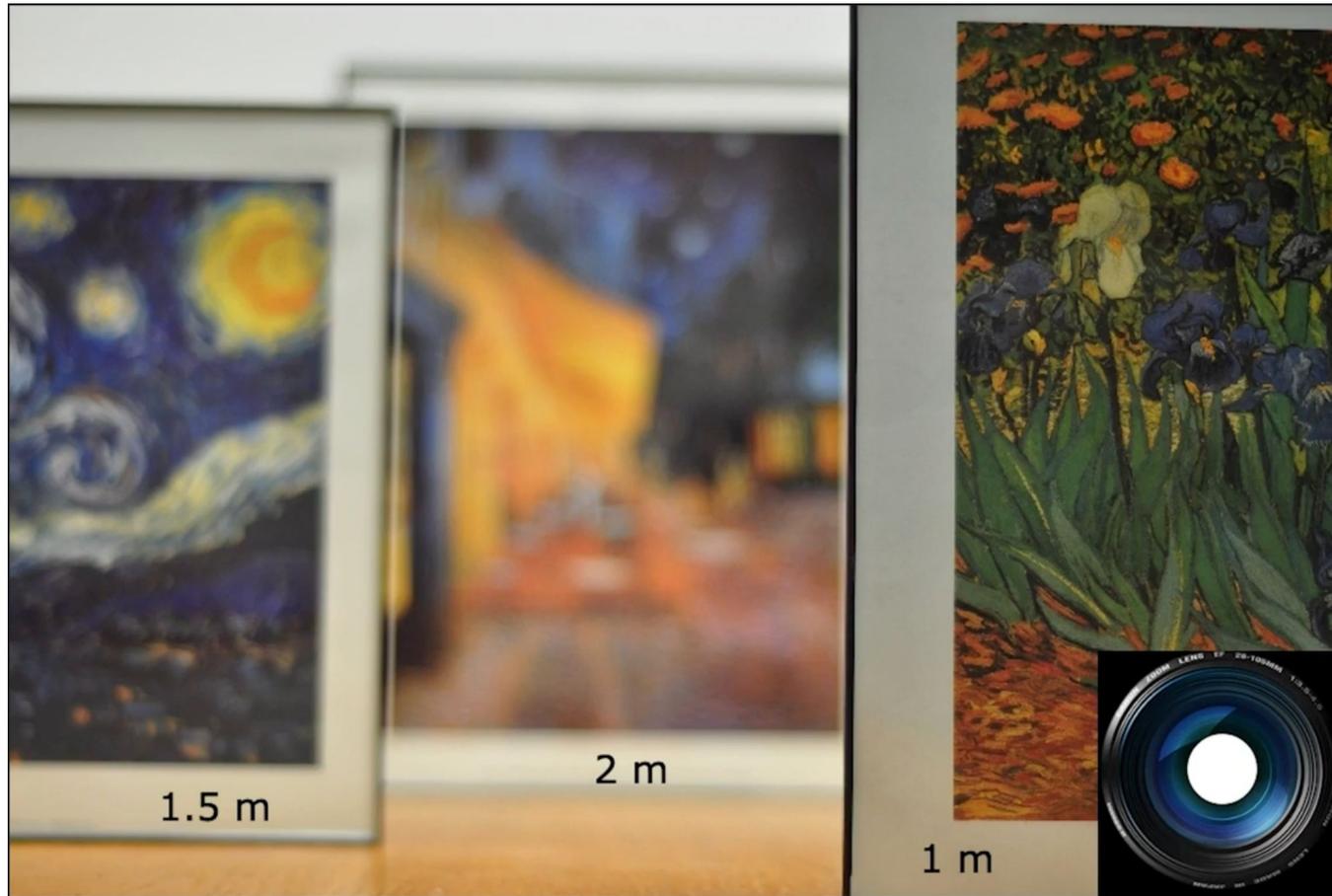


# Example (Reducing aperture)



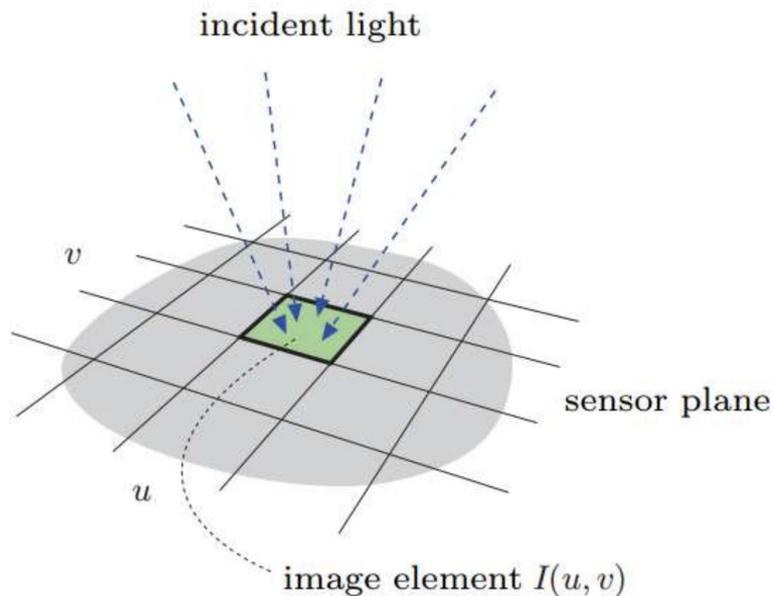
**f/16**  
Ajustando  
intensidad  
digitalmente

# Example (Reducing aperture)

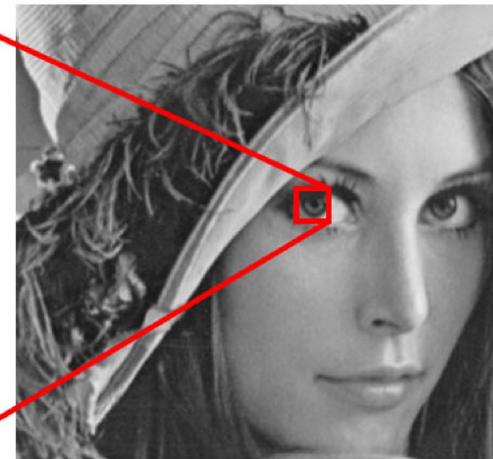


**Imagen digital**

# ¿Qué es una imagen digital?



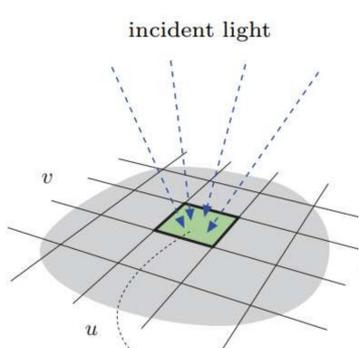
12	12	11	13	12
12	13	10	12	11
13	12	11	14	10
11	14	12	13	12
12	13	13	14	10



La proyección en el plano imagen de una cámara es una distribución continua de energía luminosa bidimensional, dependiente del tiempo.

Imagen = Matriz de números  
(cada número es un pixel)

# Del dominio continuo al dominio digital



Muestreo espacial

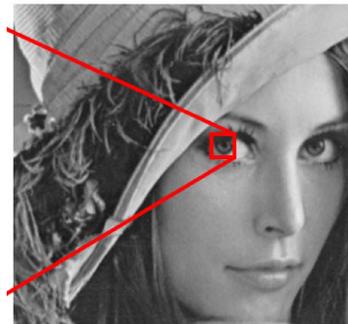
Conversión de la señal continua a su representación discreta

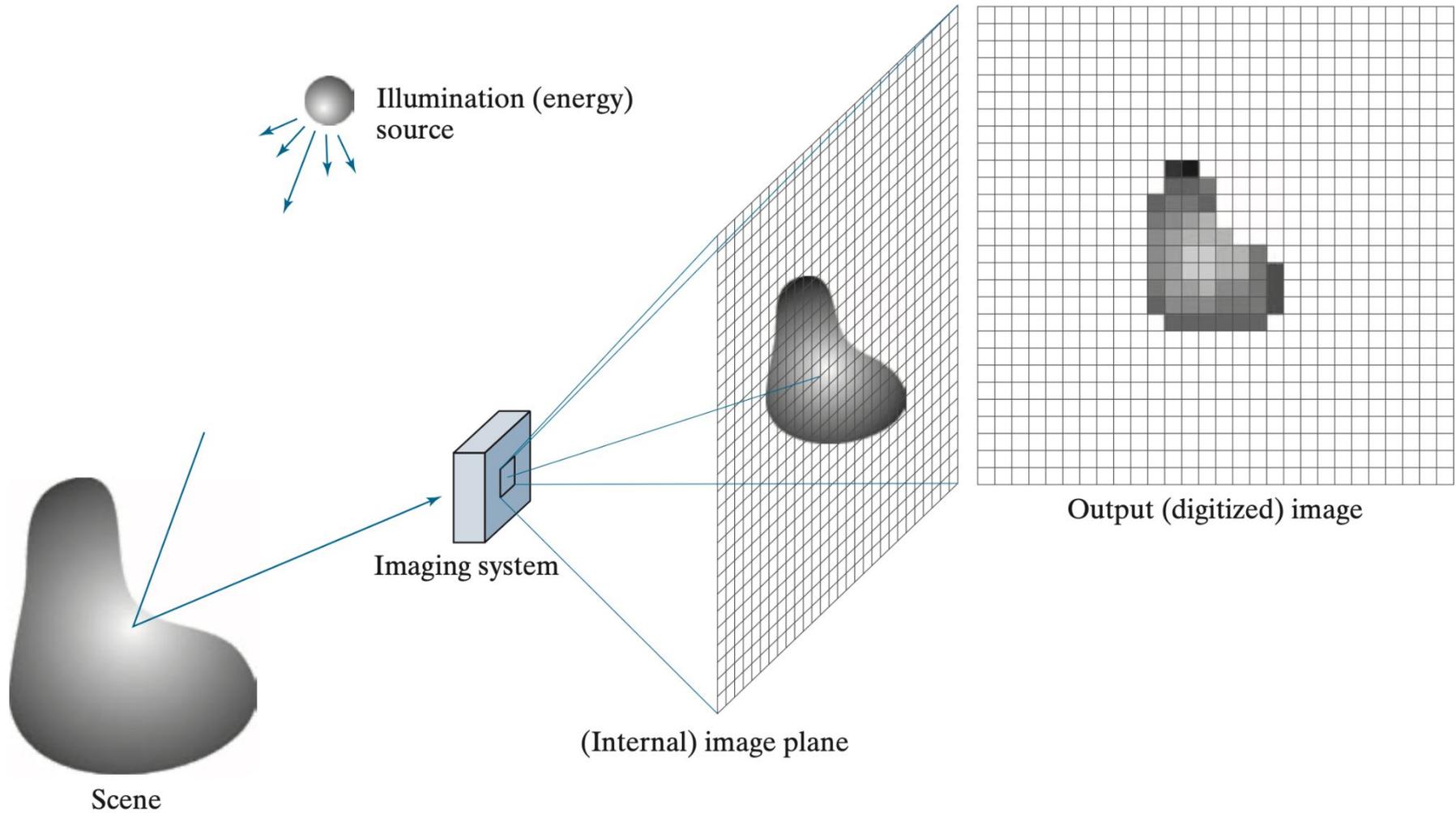
Muestreo temporal

Integra la cantidad de luz que incide en cada pixel a intervalos regulares

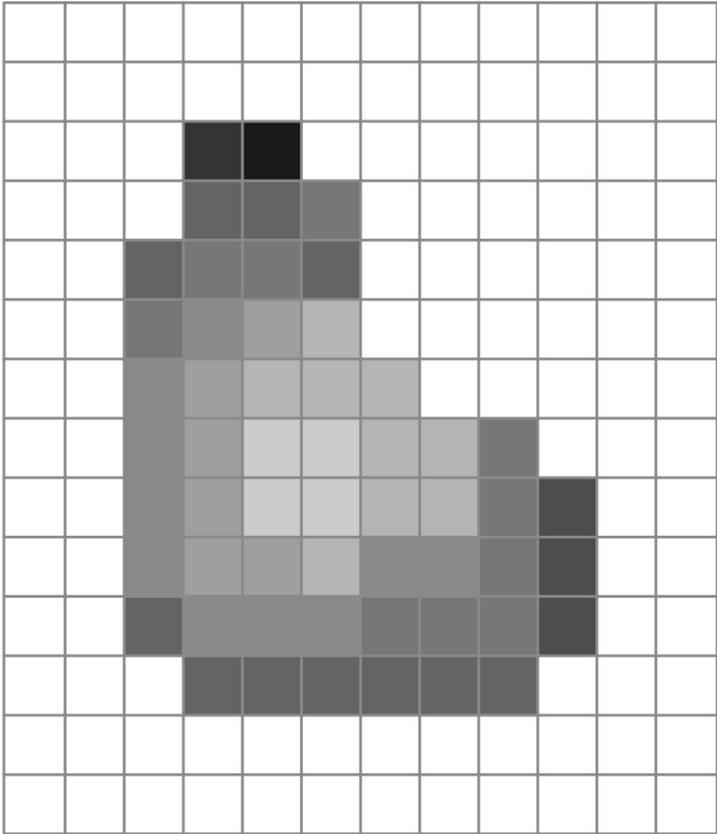
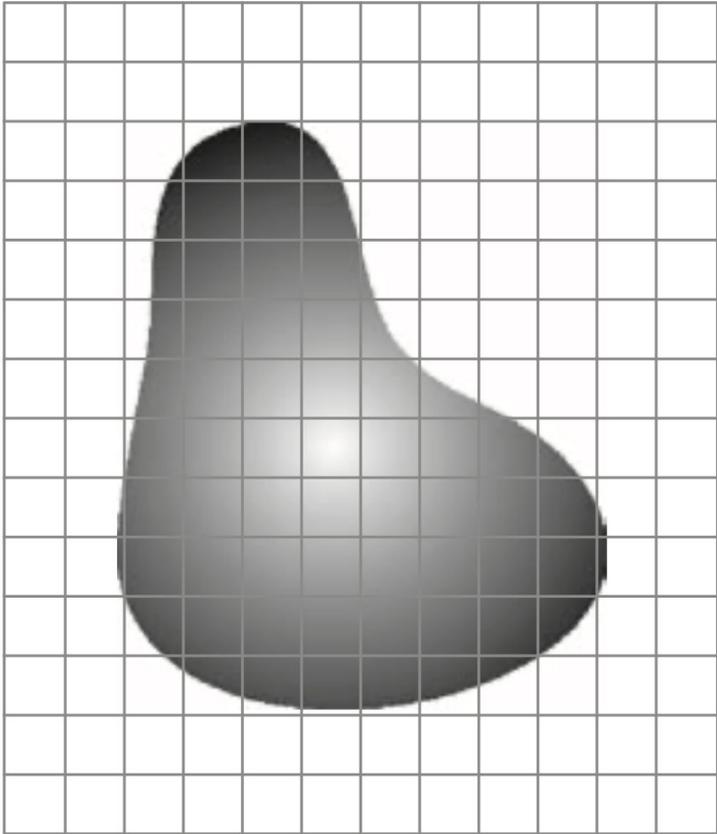
Cuantización

Los valores de la imagen se convierten a una escala de números enteros





# Del dominio continuo al dominio digital



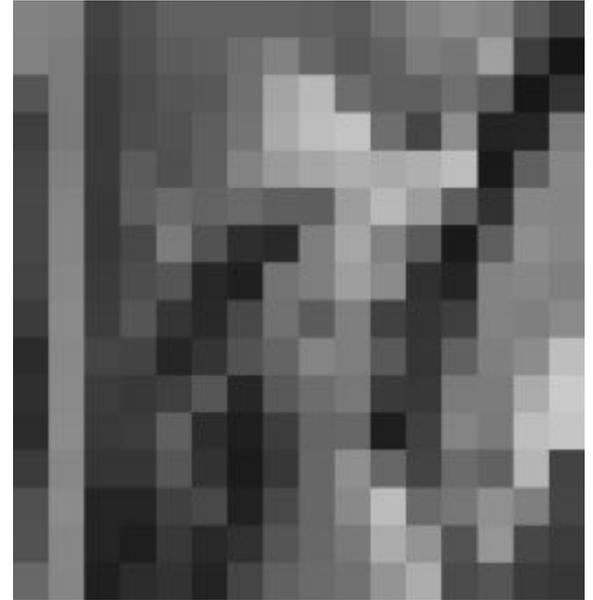
# Efecto del número de píxeles en el muestreo



256x256



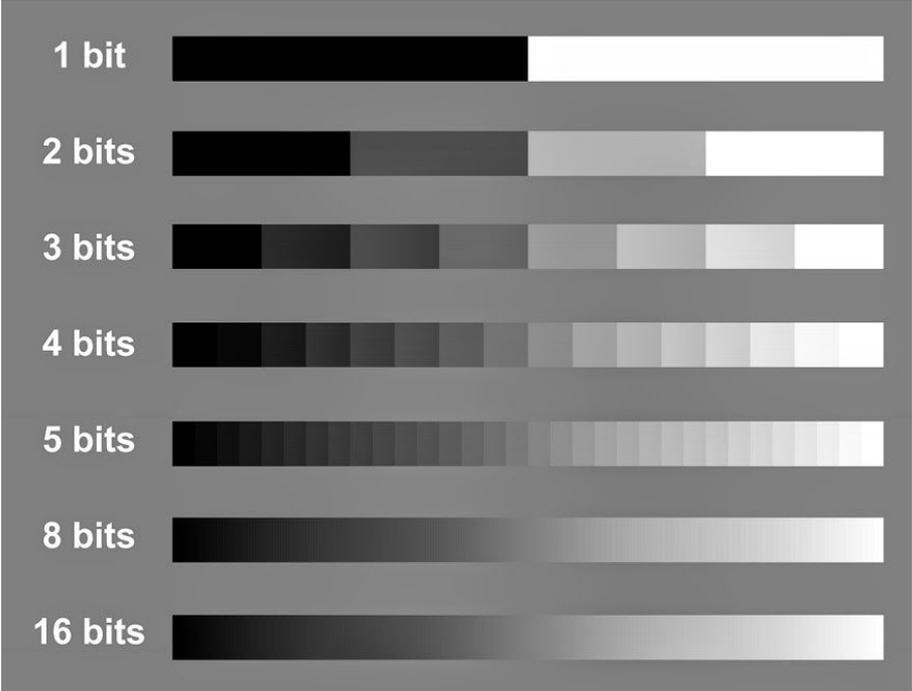
64x64



16x16

<https://www.microscopyu.com/tutorials/spatial-resolution-in-digital-imaging>

# Profundidad de bits = Tonos de gris



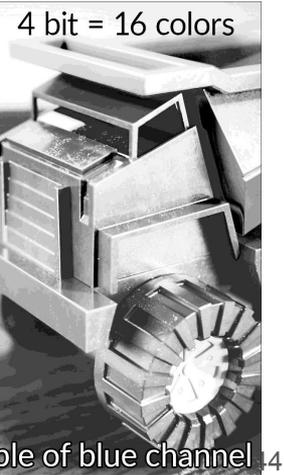
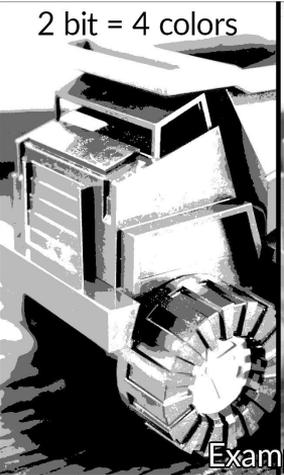
$X$  bit depth =  $2^X$  levels



1-bit

4-bit

8-bit



Example of blue channel .4

# Tipos de imágenes = Proyecciones de la función plenóptica

Binaria



Escala de grises



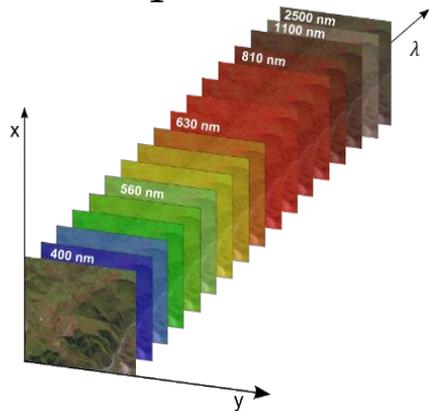
Color



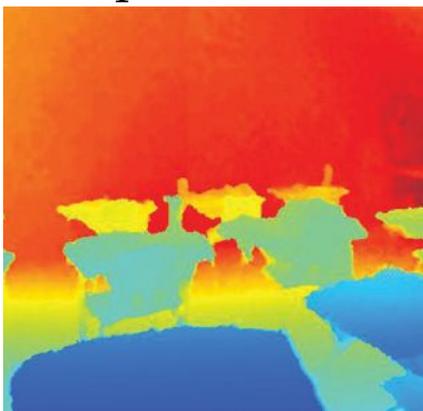
Video



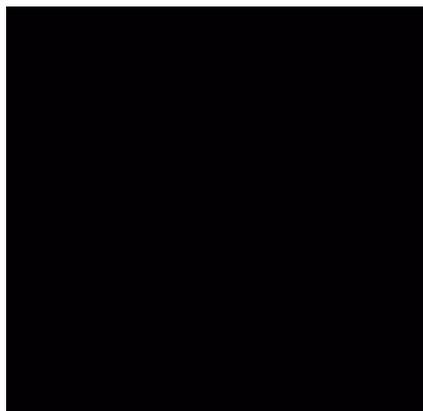
Espectral



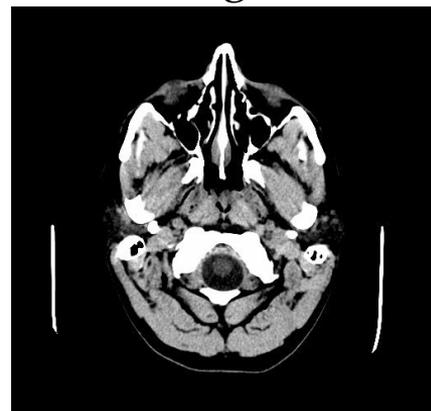
De profundidad



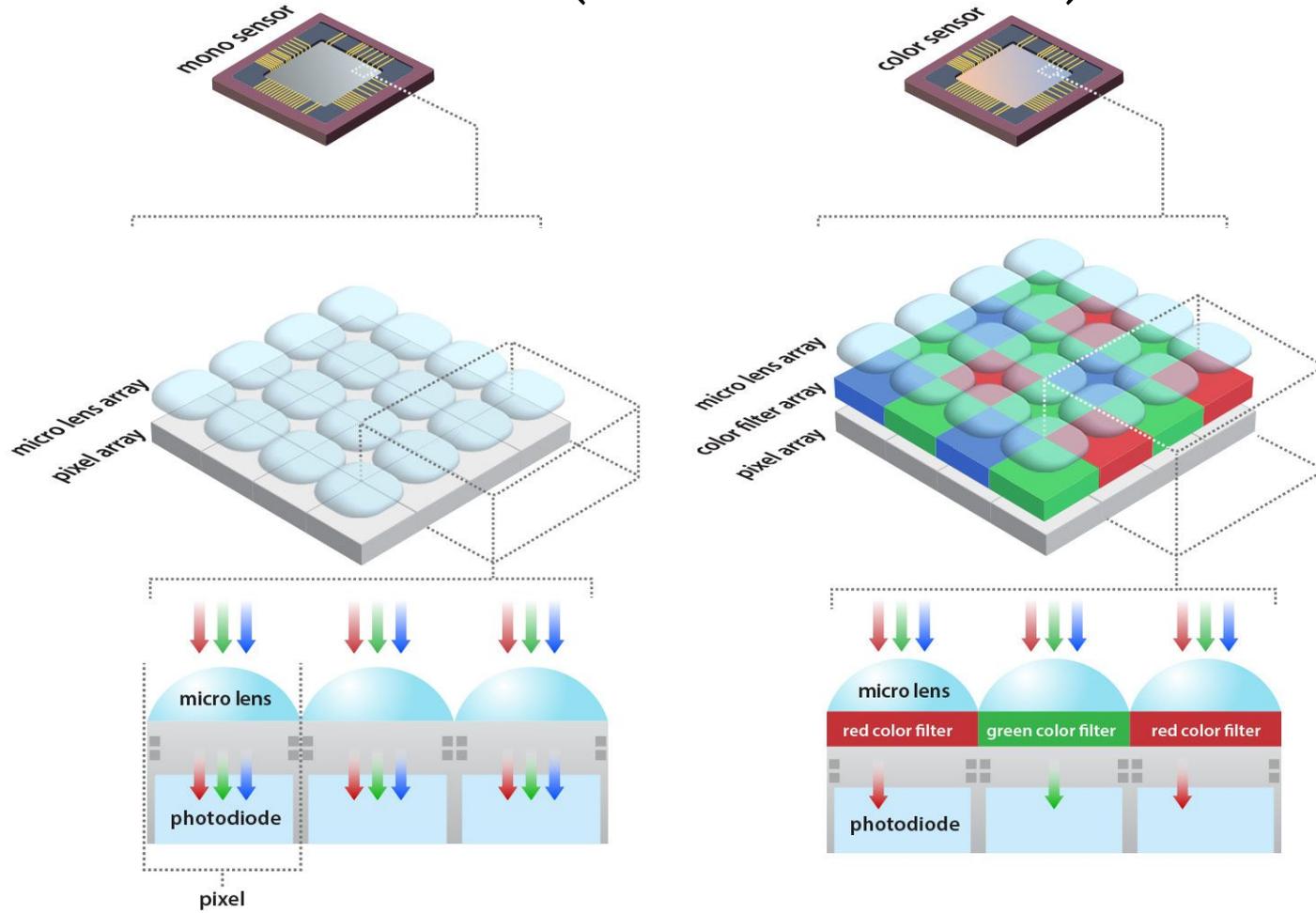
Térmica



Tomografía



# Anatomía de un sensor (Mono vs Color)



# Anatomía de un sensor

**A - Colour filter array:** Mosaic Bayer Filter.

**B - Low-pass filter/Anti-aliasing filter:** Prevent aliasing.

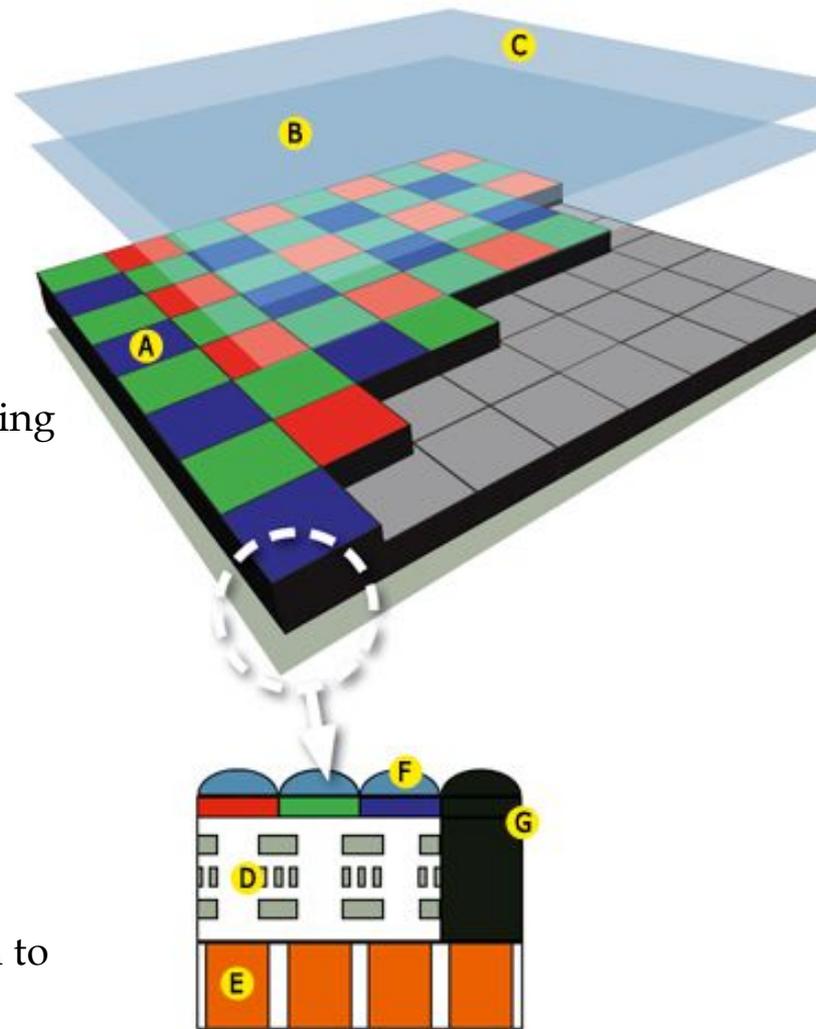
**C - Infrared filter (hot mirror):** Prevents IR light from reaching the sensor, and helps minimise any colour casts or artefacts

**D - Circuitry:** CCD vs CMOS.

**E - Pixel:** Contains a light sensitive photodetector, which measures the amount of light (photons) falling onto it.

**F - Microlenses:** Help funnel light into each pixel, thereby increasing the sensitivity of the sensor.

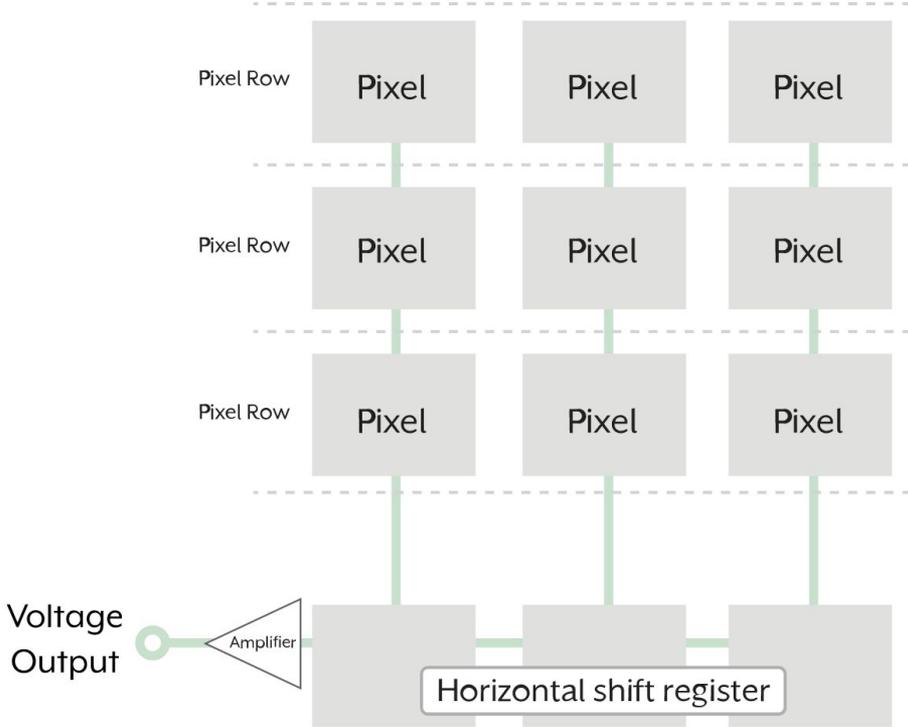
**G - Black pixels:** Around the peripheries, allows the camera to see how much dark current builds up during an exposure.



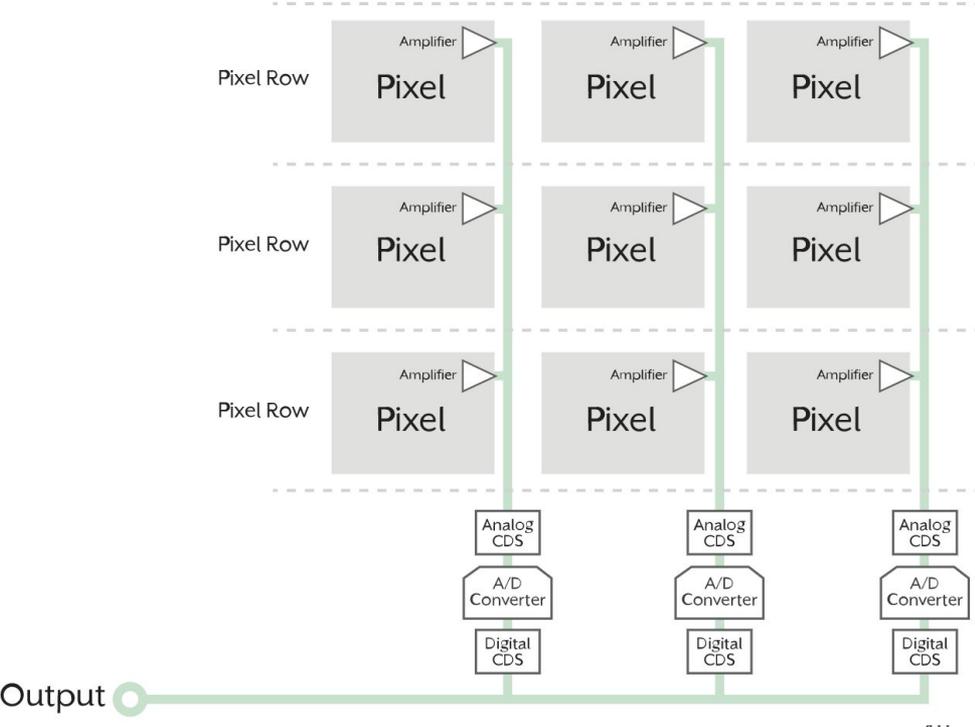
# De fotones a pixeles: CCD vs CMOS

Diferencia principal: Electrónica por pixel o global

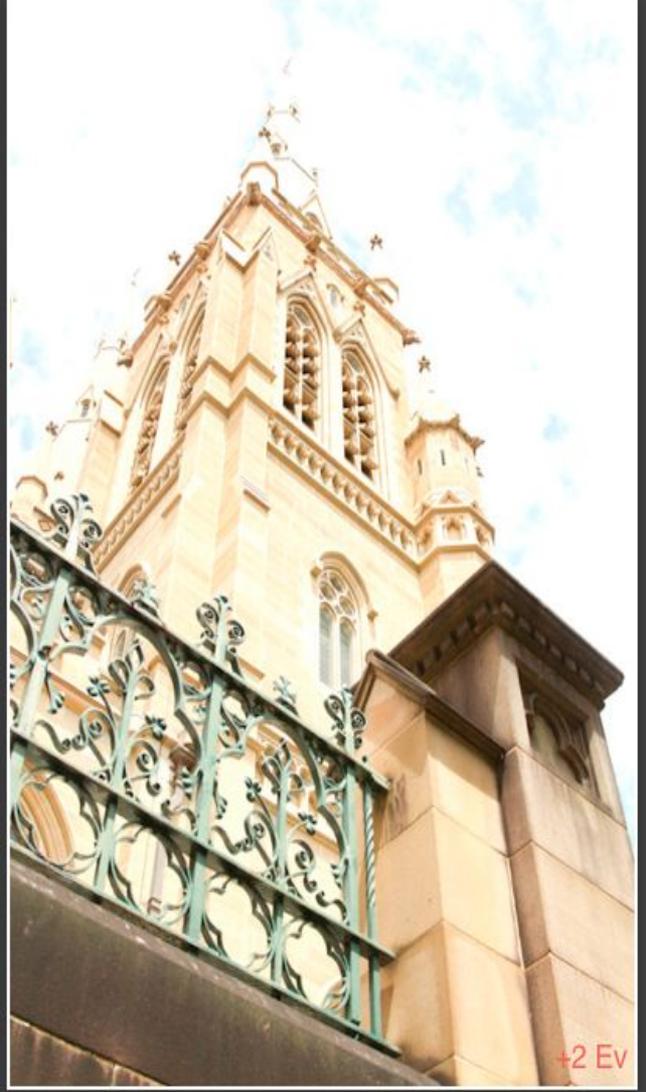
## CCD: Charged Coupled Device



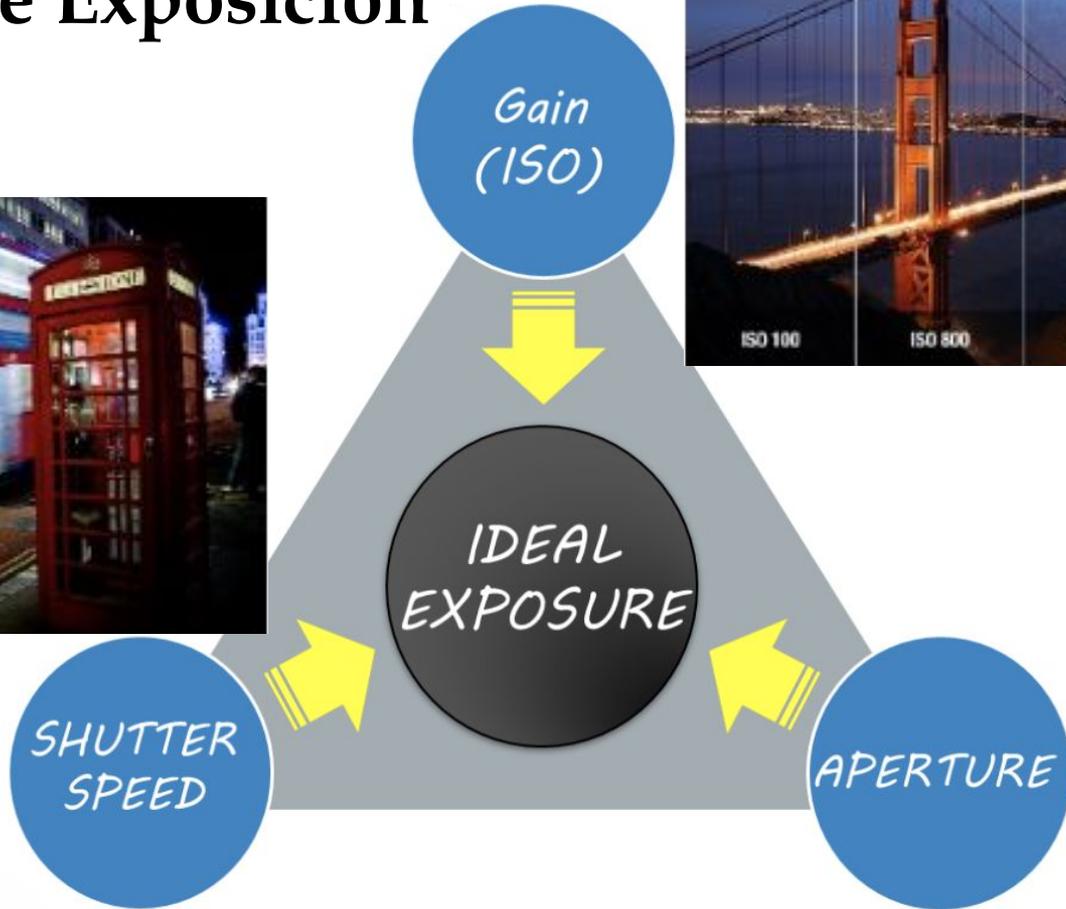
## CMOS: Complementary Metal-Oxide Semiconductor



### **3. El triángulo de la exposición**



# Triángulo de Exposición



Less Light

4000  
2000  
1000  
500  
250  
125  
60  
30  
15  
8

Shutter

Aperture



Good Exposure



ISO

100 200 400 800 1600 3200 6400 12800



f/22  
f/16  
f/11  
f/8  
f/5.6  
f/4  
f/2.8

More Light

Less Light

4000  
2000  
1000  
500  
250  
125  
60  
30  
15  
8

Shutter

Aperture

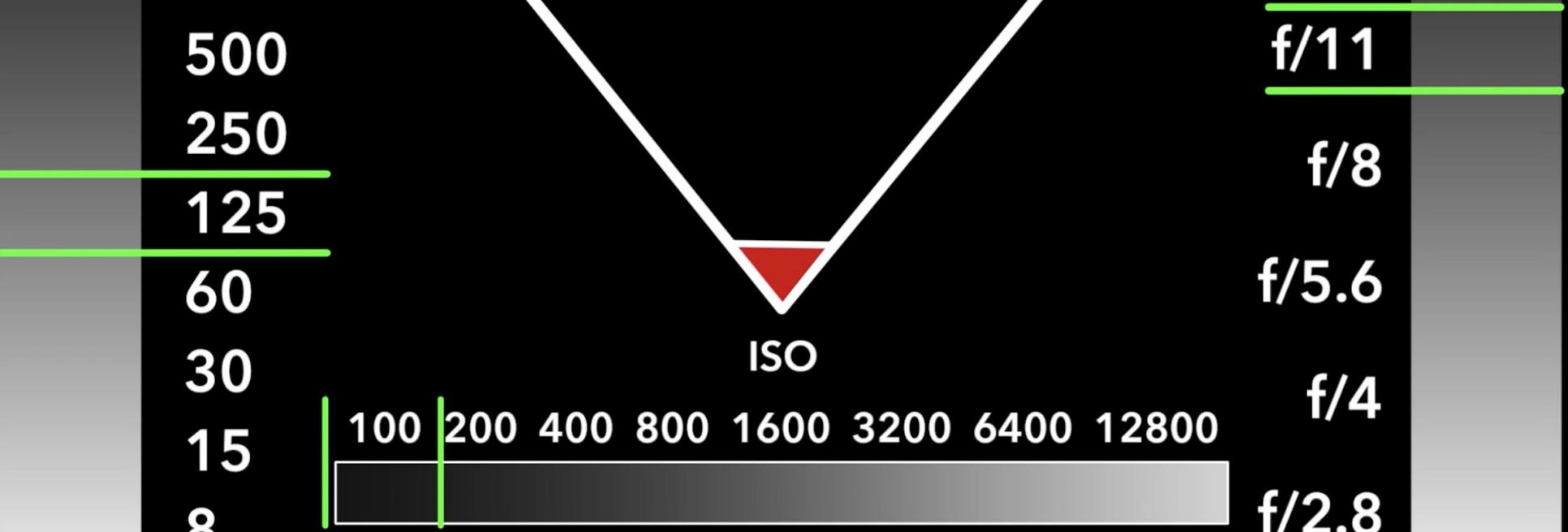
f/22  
f/16  
f/11  
f/8  
f/5.6  
f/4  
f/2.8

1 Stop Over Exposed

ISO

100 200 400 800 1600 3200 6400 12800

More Light



Less Light

4000  
2000  
1000  
500  
250  
125  
60  
30  
15  
8

Shutter

Aperture

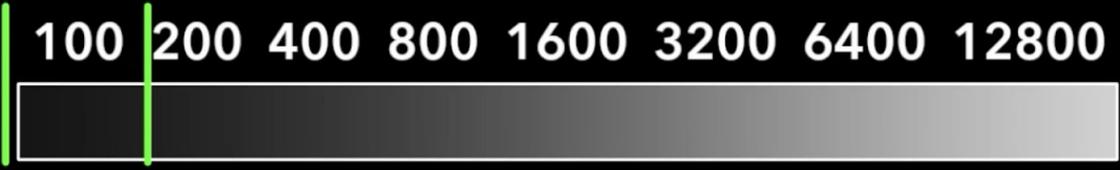
f/22  
f/16  
f/11  
f/8  
f/5.6  
f/4  
f/2.8

Good Exposure

ISO

100 200 400 800 1600 3200 6400 12800

More Light



Less Light

4000

2000

1000

500

250

125

60

30

15

8

Shutter

Aperture

Good Exposure

ISO

f/22

f/16

f/11

f/8

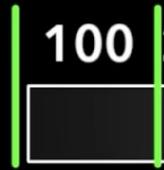
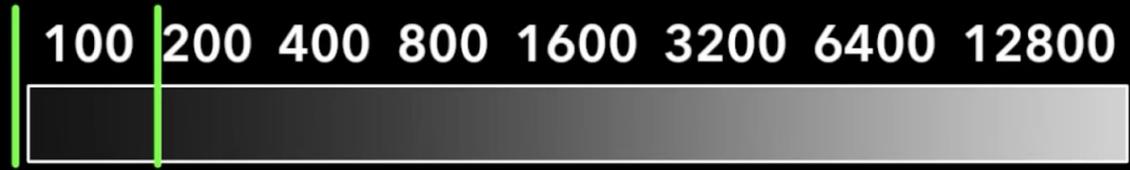
f/5.6

f/4

f/2.8

100 200 400 800 1600 3200 6400 12800

More Light



Less Light

4000  
2000  
1000  
500  
250  
125  
60  
30  
15  
8

Shutter

Aperture

f/22  
f/16  
f/11  
f/8  
f/5.6  
f/4  
f/2.8

2 Stops Under Exposed

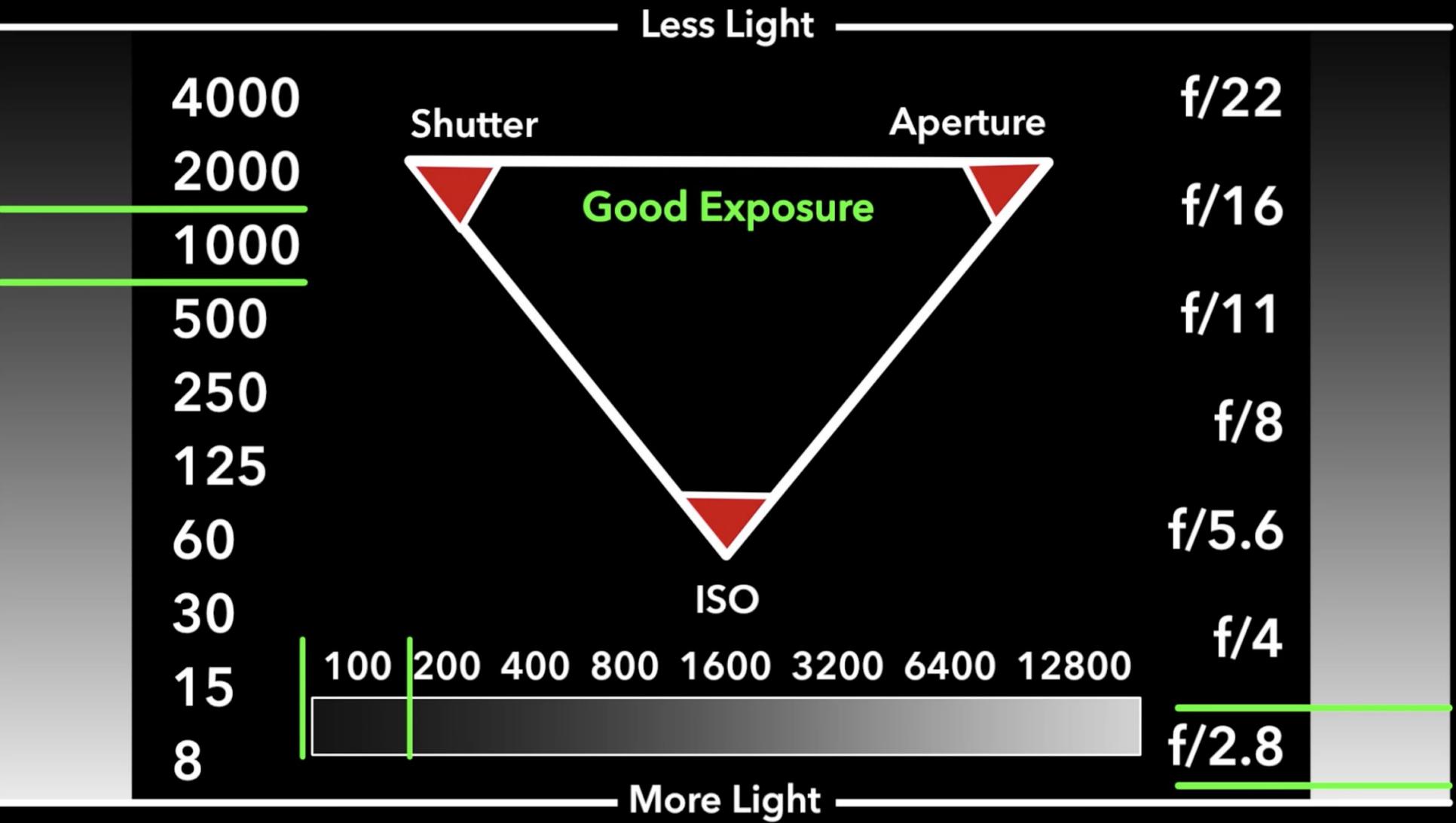


ISO

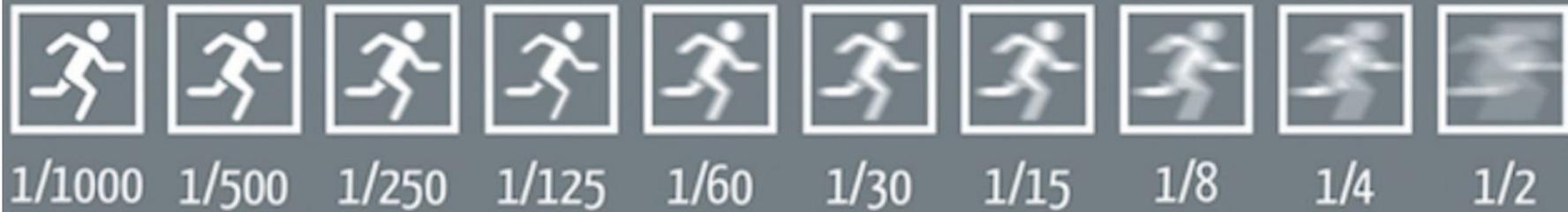
100 200 400 800 1600 3200 6400 12800

More Light





# Shutter Speed



1 sec



1/4 sec



1/15 sec



1/60 sec



1/160 sec



1/750 of a second



1/125 of a second



1/10 of a second



0.7 of a second

# Apertura



$$\pi r_1^2 = A$$
$$\pi r_2^2 = 2A$$

$$\sqrt{\cancel{\pi} r_2^2} = \sqrt{2(\cancel{\pi} r_1^2)}$$
$$r_2 = \sqrt{2} r_1$$

or 1.41421  $r_1$

**Large f/#**



**Small f/#**



# Gain (ISO)



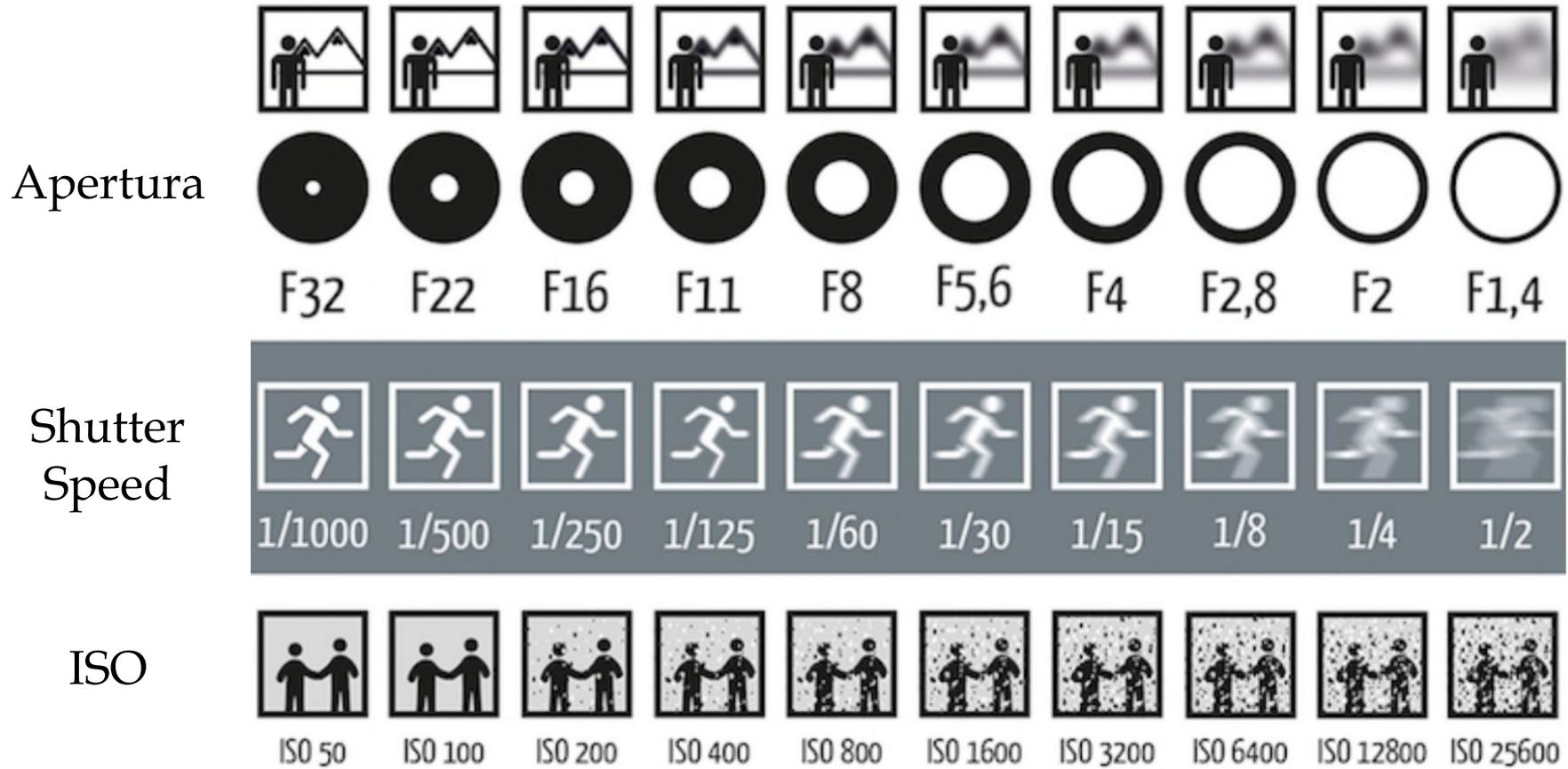
ISO 100

ISO 3200

CLEAN IMAGE

NOISY IMAGE

# Triángulo de la exposición = Trade-off



Try it yourself

<https://camerasim.com/original-camerasim/>

*CameraSim*

**Camera simulators for photography  
instructors & their students.**

# Try it yourself

<http://photography-mapped.com/interact.html>



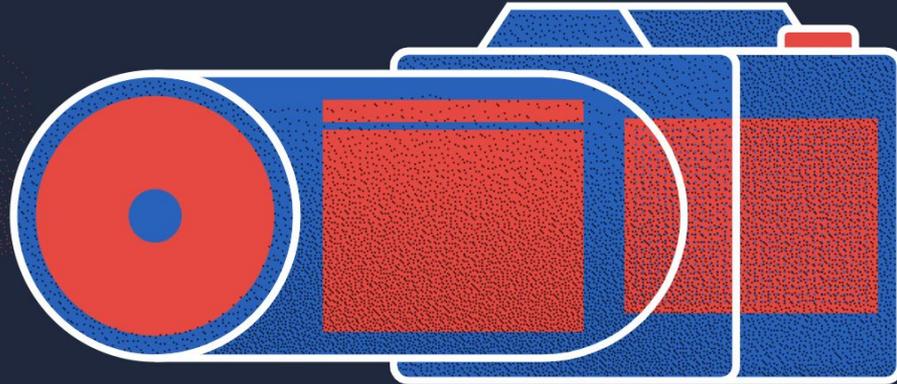
Photography Mapped

Interact

Graphic

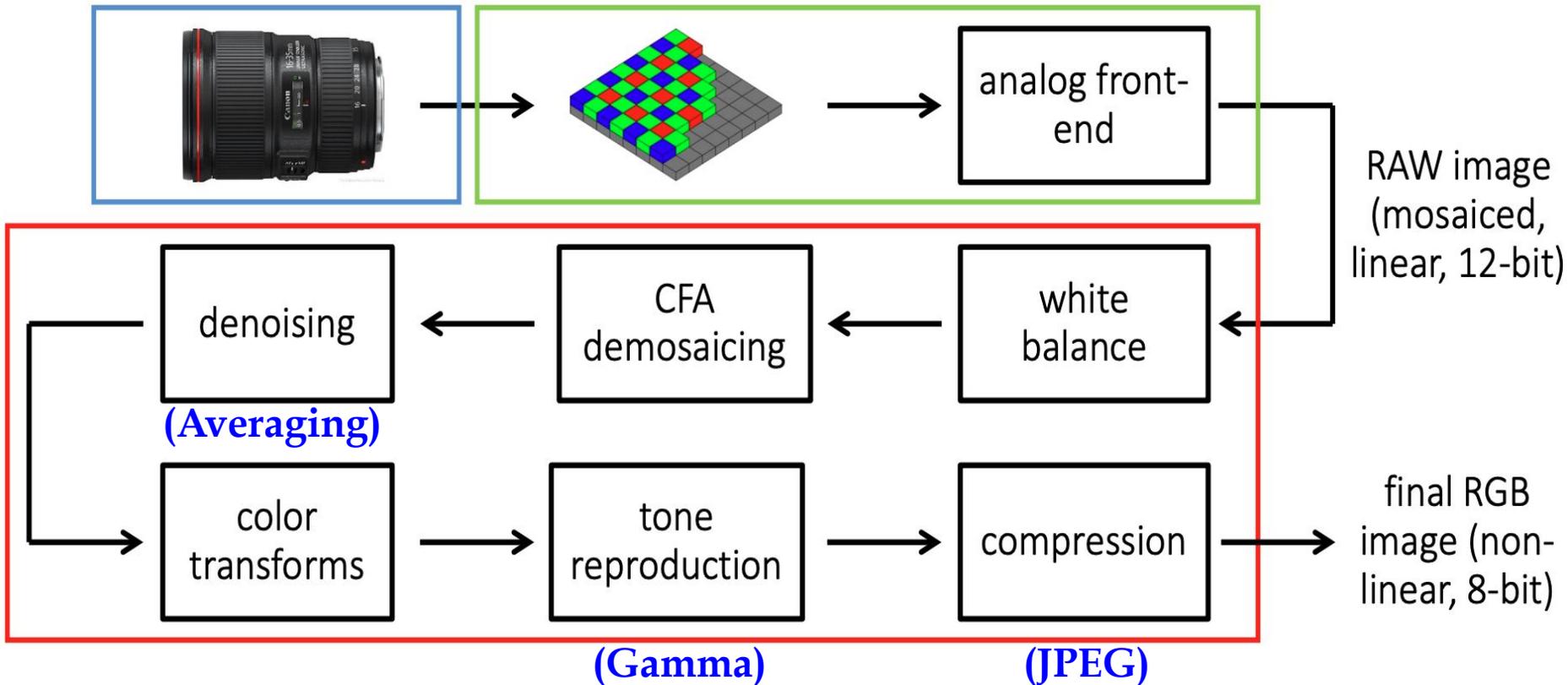
About

- Auto / Manual -



## **4. Pipeline de procesamiento de imágenes digitales (en cámara)**

# The (in-camera) image processing pipeline



# Balance de Blancos

Human visual system has *chromatic adaptation*:

- We can perceive white (and other colors) correctly under different light sources.

Retinal vs  
perceived color.



[Slide credit: Todd Zickler]

# Fun fact



## ORIGINAL

(Blue and Gold)  
+0% brightness, +0%  
contrast



## DARKER

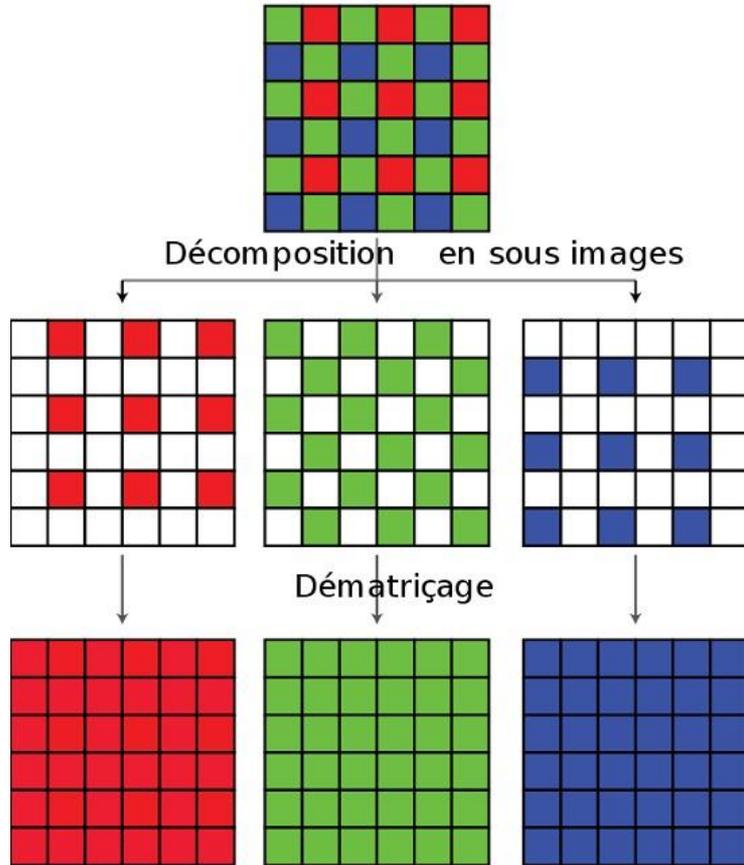
(Blue and Black)  
-30% brightness, +40%  
contrast



## BRIGHTER

(White and Gold)  
+40% brightness, +40%  
contrast

# Demosaicking



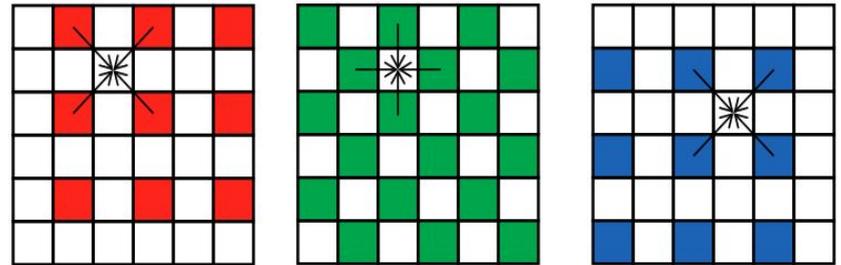
- Interpolación bilineal (método simple)

$$G_7 = \frac{G_1 + G_2 + G_3 + G_4}{4}$$

- Se usan métodos más avanzados

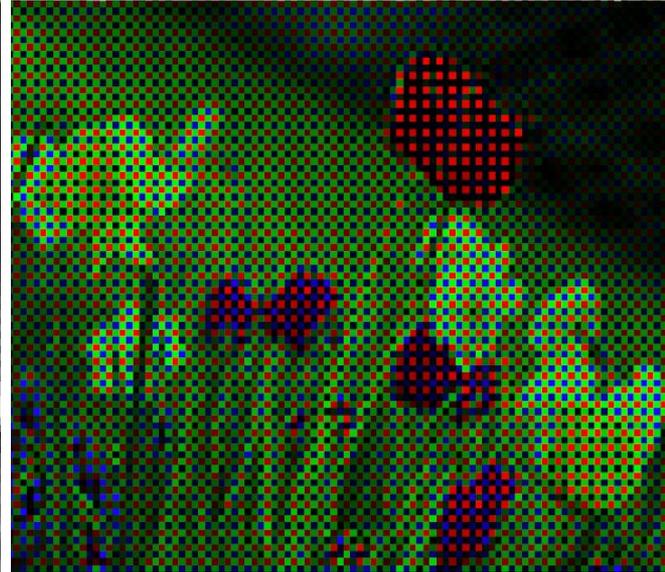
- Menon
- Malvar
- Freeman, Etc.

- $\frac{2}{3}$  partes de los datos son “inventados”



# Demosaicking (Raw Data)

G	R	G	R	G	R	G	R
B	G	B	G	B	G	B	G
G	R	G	R	G	R	G	R
B	G	B	G	B	G	B	G
G	R	G	R	G	R	G	R
B	G	B	G	B	G	B	G
G	R	G	R	G	R	G	R
B	G	B	G	B	G	B	G



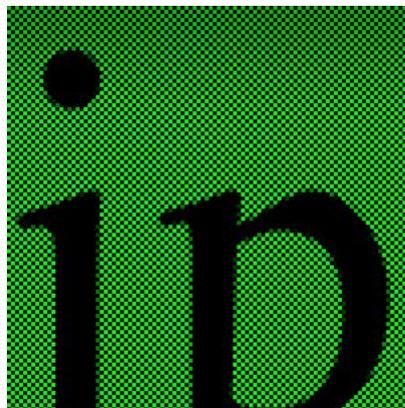
# Demosaicking (Interpolation Example)



Raw image



Red channel



Green channel



Blue channel

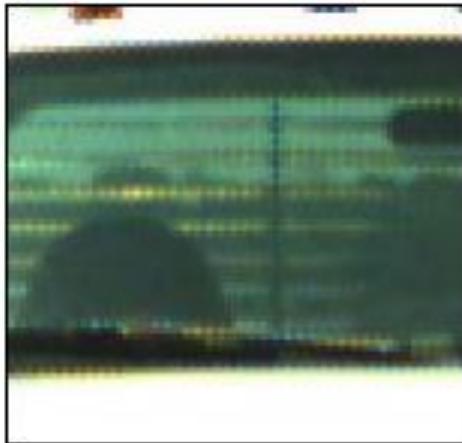
Ground truth



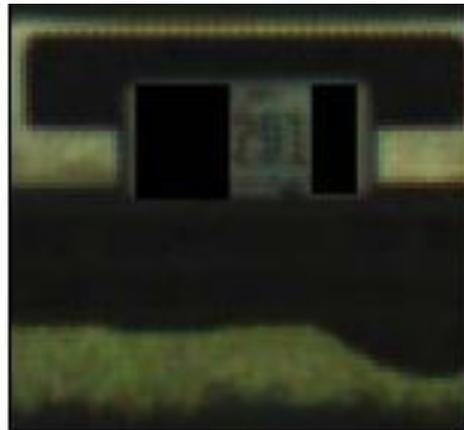
Demosaicked

# Problemas

Artefactos  
de color  
falso



Artefacto  
de  
cremallera



# Denoising (Tipos de ruido)

## 1) Ruido de disparo (fotónico):

Las tasas de llegada de fotones son un proceso aleatorio (Poisson)

## 2) Ruido oscuro:

Electrones debido a la actividad térmica (empeora cuando el sensor se calienta)

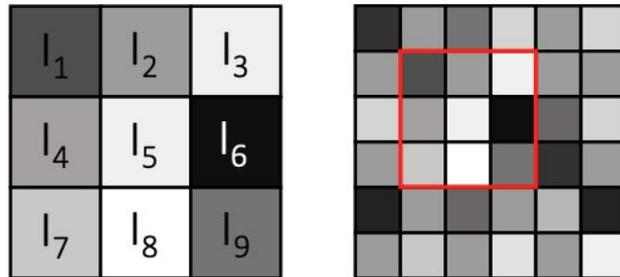
## 3) Ruido de lectura:

Causado por la lectura y la electrónica AFE (por ejemplo, ganancia, conversor A/D)



# Denoising (Eliminación de ruido)

Look at the neighborhood around you.



- Mean filtering (take average):

$$I'_5 = \frac{I_1 + I_2 + I_3 + I_4 + I_5 + I_6 + I_7 + I_8 + I_9}{9}$$

- Median filtering (take median):

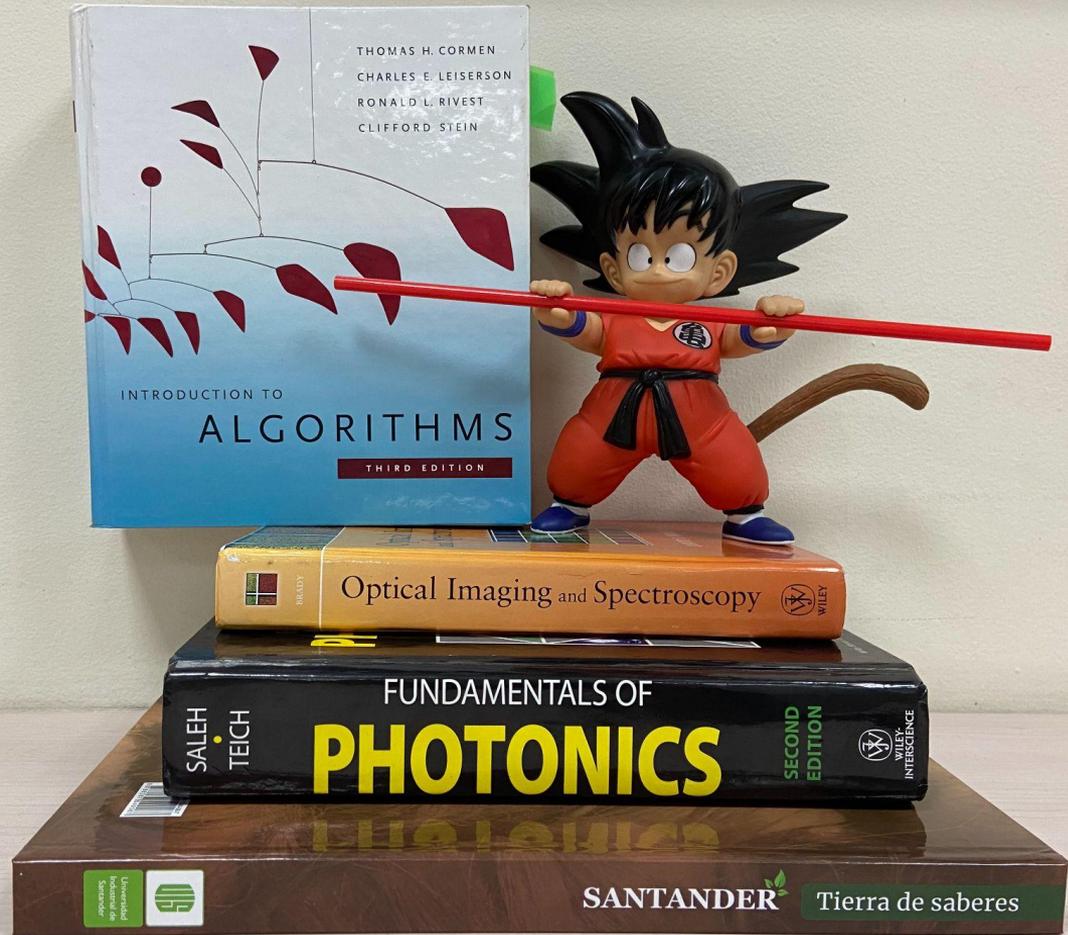
$$I'_5 = \text{median}(I_1, I_2, I_3, I_4, I_5, I_6, I_7, I_8, I_9)$$

Large area of research. We will see some more about filtering in a later lecture.

# Diferentes cámaras generan diferentes imágenes



# Ejemplo





iPhone XR



iPhone 11



iPhone 13



Xiaomi 9S



Samsung A30





**iPhone XR**



**iPhone 11**



**iPhone 13**



**Xiaomi 9S**



**Samsung A30**

# **5. Transformaciones de imágenes**

# ¿Qué es una transformación geométrica?

- Usadas para modificar la disposición espacial de los píxeles de una imagen.
- Las T.G. constan de dos operaciones básicas:
  - a. Transformación espacial de coordenadas.
  - b. Interpolación de intensidad, que asigna valores de intensidad a los píxeles transformados espacialmente.

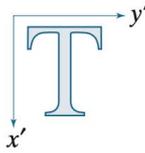
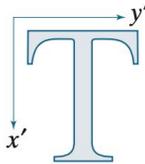
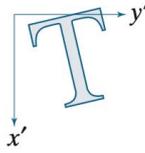
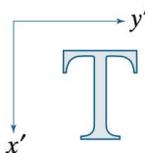
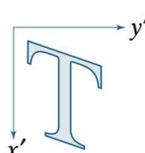
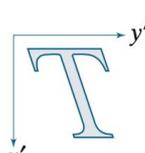
## Transformación de coordenadas

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \mathbf{T} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} \\ t_{21} & t_{22} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## Transformación afín de coordenadas

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \mathbf{A} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Puede escalar, rotar, mover o estirar una imagen.

Transformation Name	Affine Matrix, A	Coordinate Equations	Example
Identity	$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= x \\ y' &= y \end{aligned}$	
Scaling/Reflection (For reflection, set one scaling factor to -1 and the other to 0)	$\begin{bmatrix} c_x & 0 & 0 \\ 0 & c_y & 0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= c_x x \\ y' &= c_y y \end{aligned}$	
Rotation (about the origin)	$\begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= x \cos \theta - y \sin \theta \\ y' &= x \sin \theta + y \cos \theta \end{aligned}$	
Translation	$\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= x + t_x \\ y' &= y + t_y \end{aligned}$	
Shear (vertical)	$\begin{bmatrix} 1 & s_v & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= x + s_v y \\ y' &= y \end{aligned}$	
Shear (horizontal)	$\begin{bmatrix} 1 & 0 & 0 \\ s_h & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$	$\begin{aligned} x' &= x \\ y' &= s_h x + y \end{aligned}$	

# Histograma

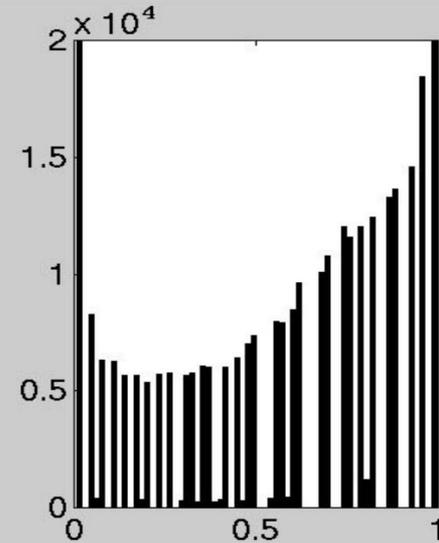
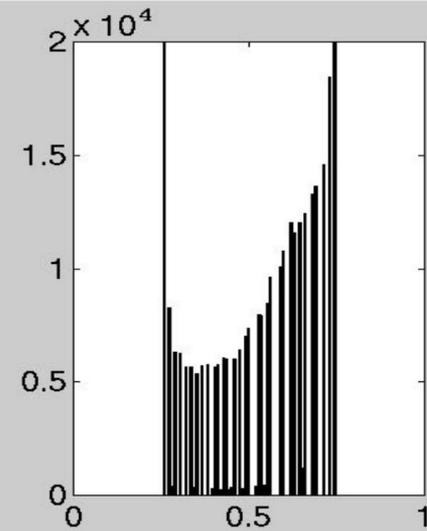
Cada entrada del histograma se define como el “Número de píxeles con el valor de intensidad  $i$ ”

$$h(i) = \text{card} \{ (u, v) \mid I(u, v) = i \}$$

$$0 \leq i < K$$

$K$  = niveles de intensidad (depende de #bits)

- $h(0)$  es el número de píxeles con el valor 0
- $h(1)$  el número de píxeles con el valor 1
- y así sucesivamente



# Transformaciones espaciales de intensidad

Pixel-a-pixel

$$s = T(r)$$

$r$  = valor del píxel de entrada

$s$  = valor del píxel de salida

$T$  = operador sobre una  
vecindad de  $1 \times 1$

De vecindario

$$g(x, y) = T[f(x, y)]$$

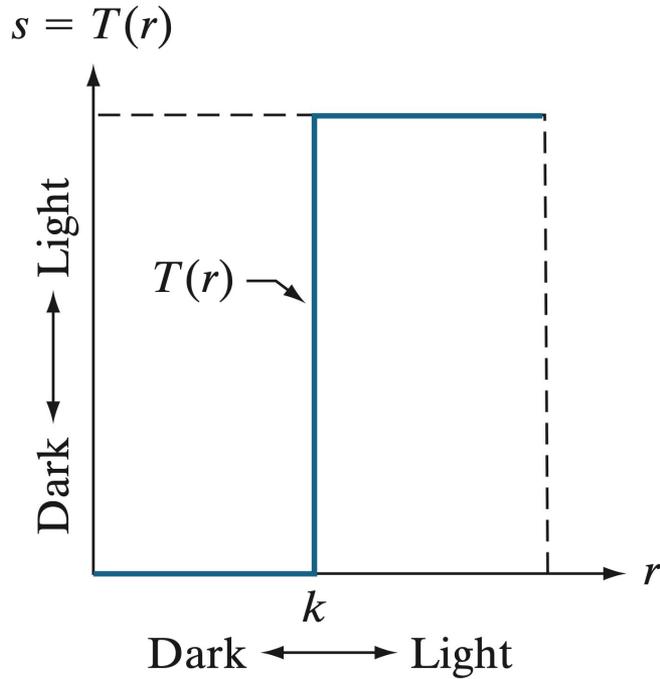
$f(x, y)$  = imagen de entrada

$g(x, y)$  = imagen de salida

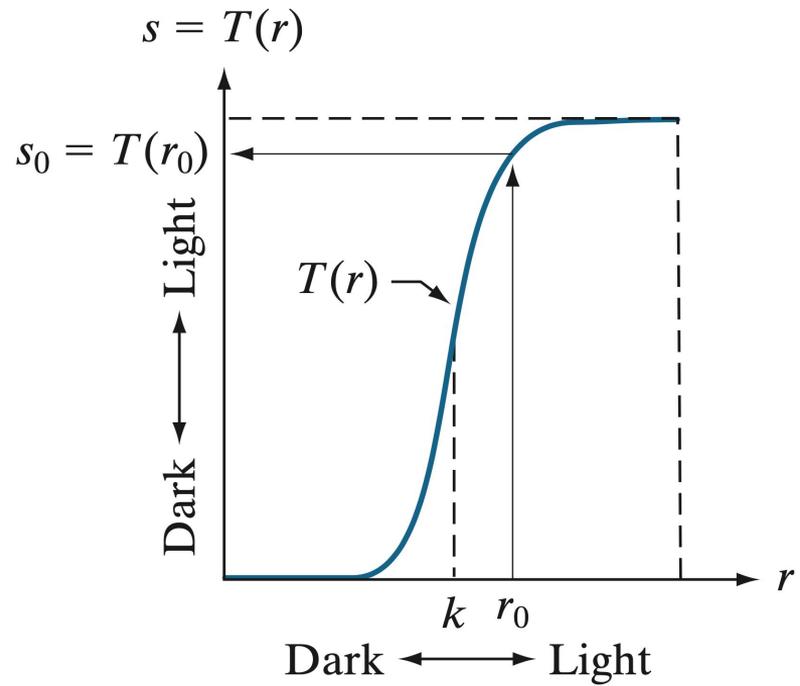
$T$  = operador en  $f$  definido sobre  
una vecindad del punto  $(x, y)$

La transformación es independiente  
de la ubicación; depende solo de la  
intensidad del píxel

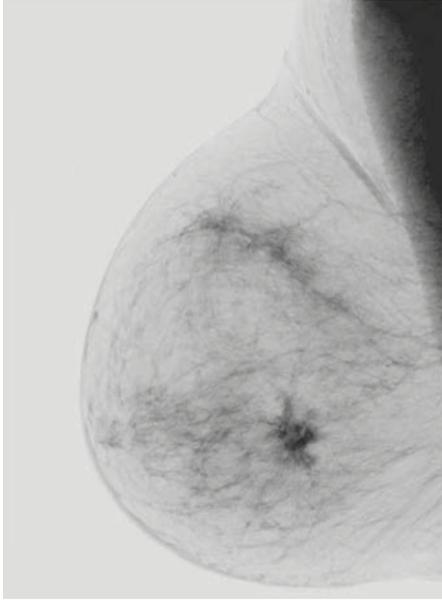
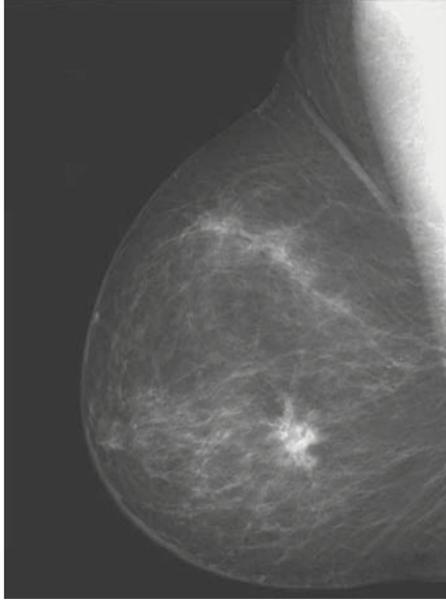
# 1. Umbralización



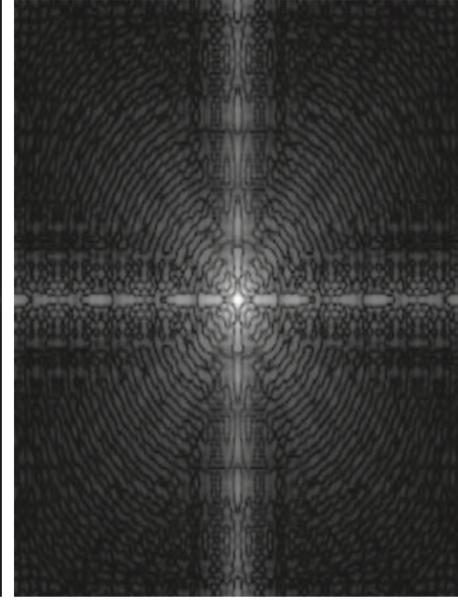
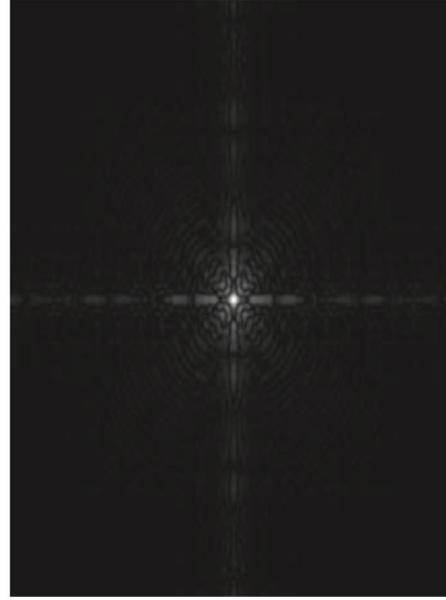
# 2. Mejoramiento de contraste



- Las T.I. son técnicas simples de procesamiento de imágenes
- Implementadas normalmente a través de Look-Up-Tables (LUT)



Negativa

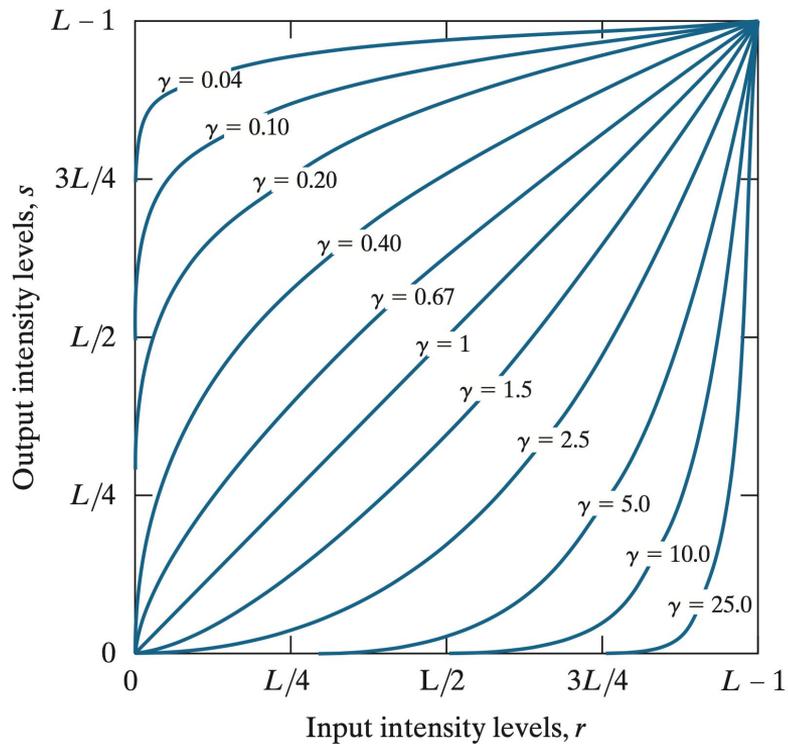


Logarítmica ( $c=1$ )

# Corrección Gamma $s = cr^\gamma$

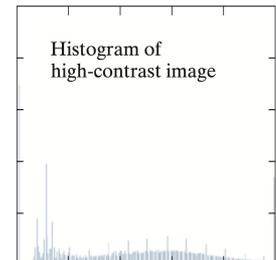
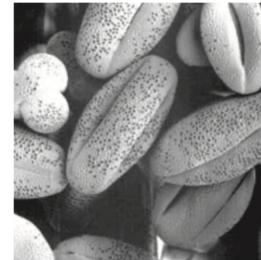
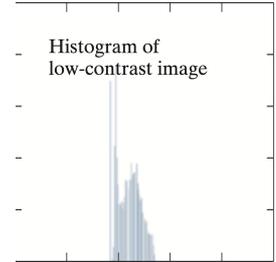
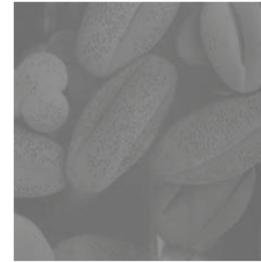
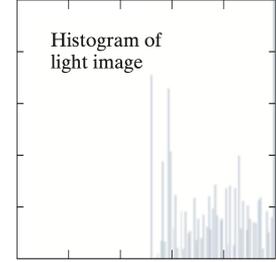
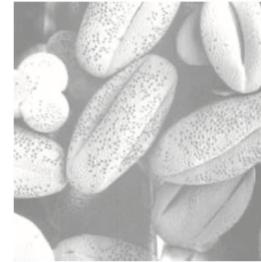
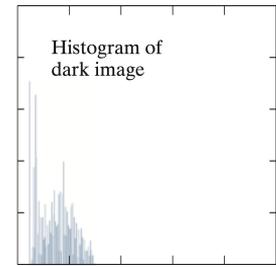
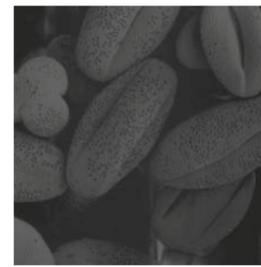
$\gamma < 1$ : Mejora áreas oscuras

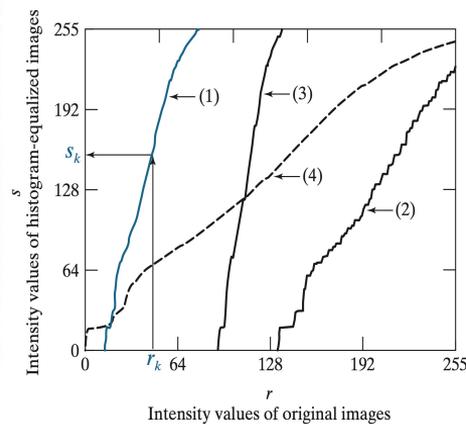
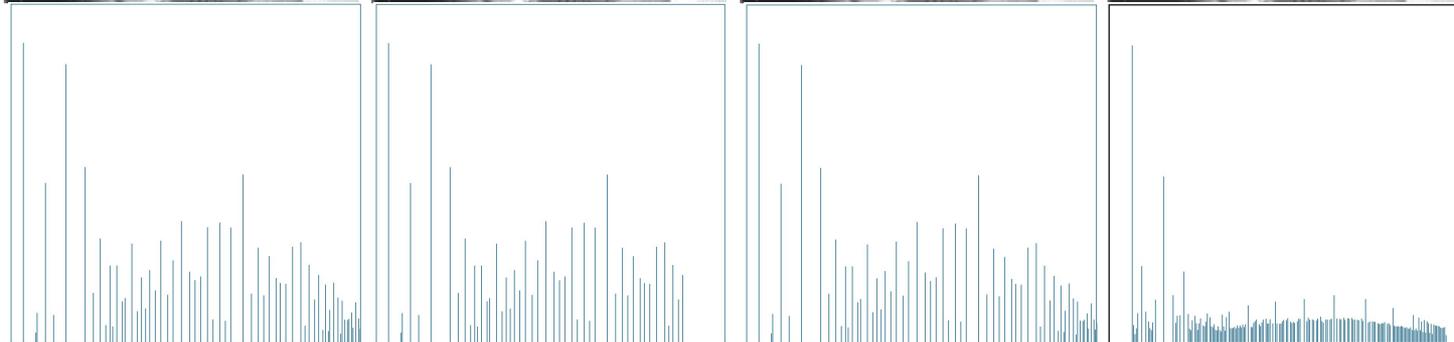
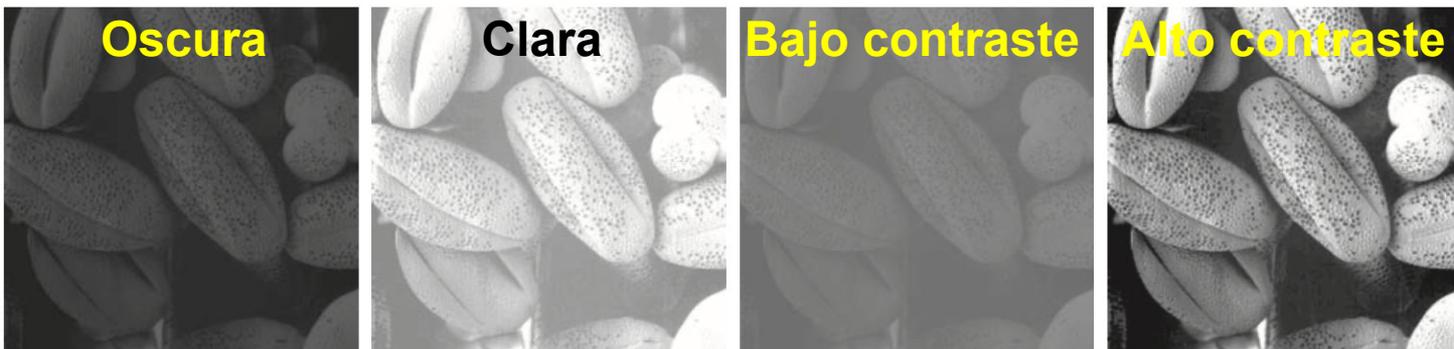
$\gamma > 1$ : Mejora áreas brillantes



# Ecualización del histograma

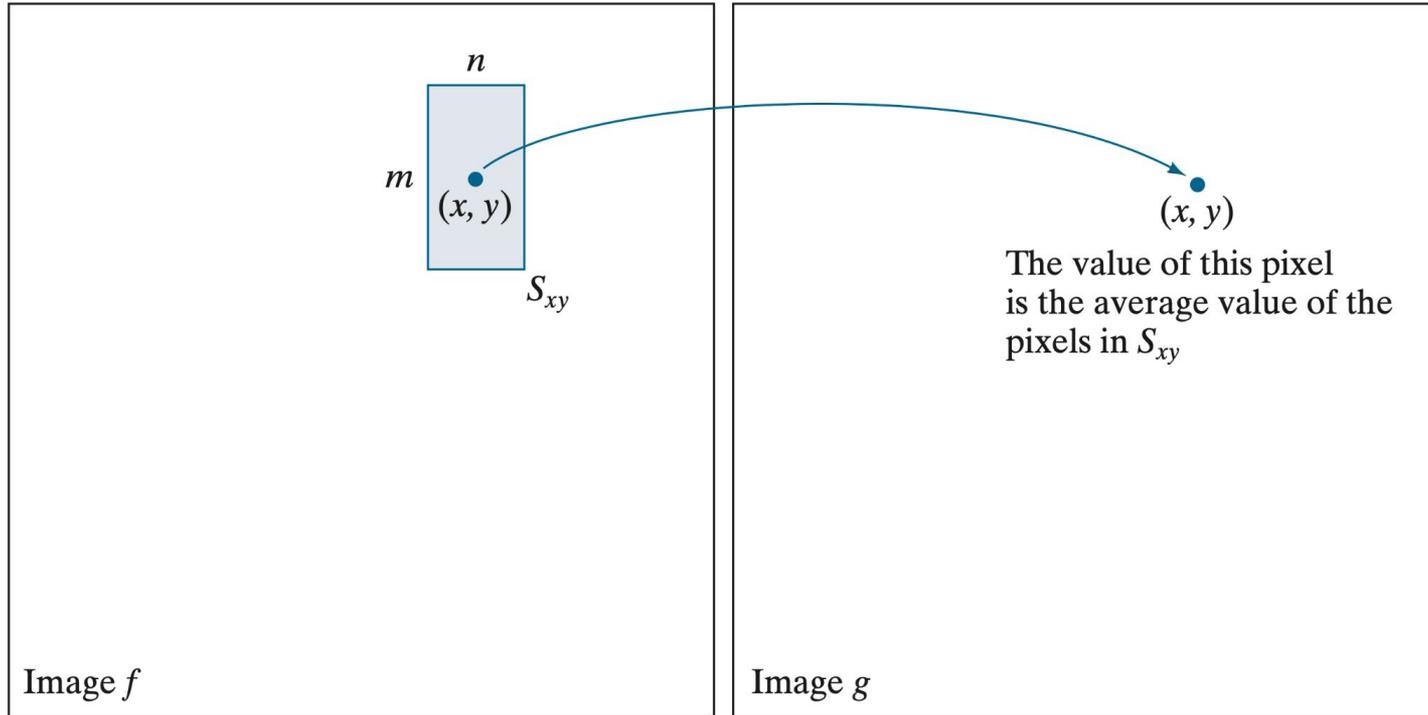
- Imágenes claras, oscuras y de bajo contraste tienen **histogramas concentrados**.
- Imágenes con histogramas uniformes
  - Contienen toda la gama de valores de gris
  - Tienen alto contraste
  - Mejor apariencia visual general





# **Transformaciones de vecindario (Convolución)**

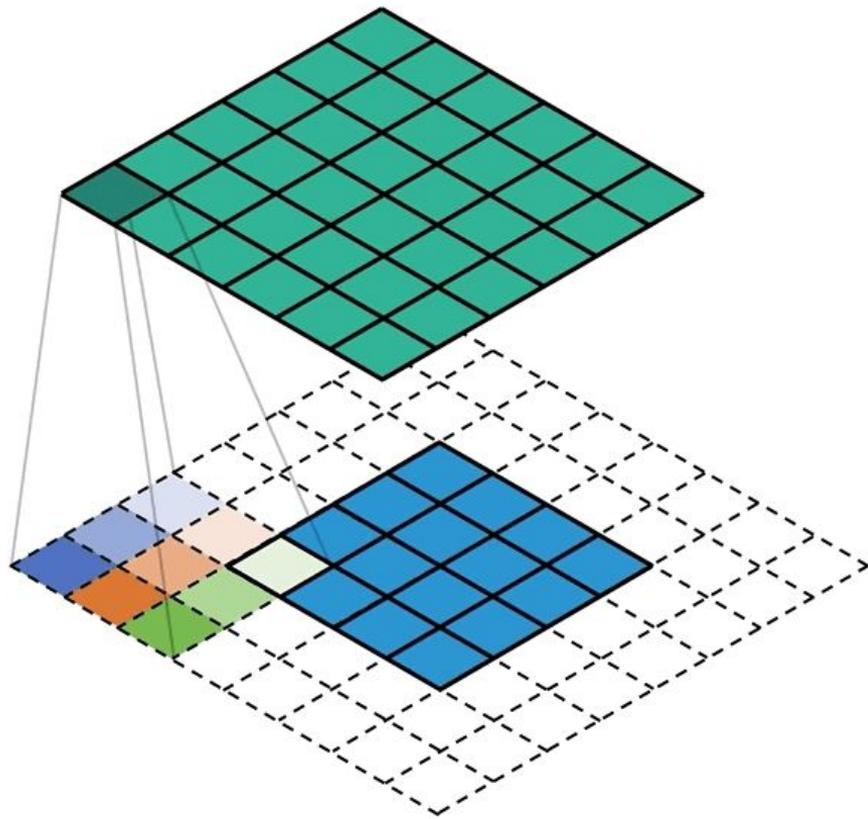
# Transformaciones de vecindario



$$g(x, y) = \frac{1}{mn} \sum_{(r, c) \in S_{xy}} f(r, c)$$

# Convolución 2D

$$g(x,y) = h(x,y) \circledast f(x,y)$$



$3_0$	$3_1$	$2_2$	1	0
$0_2$	$0_2$	$1_0$	3	1
$3_0$	$1_1$	$2_2$	2	3
2	0	0	2	2
2	0	0	0	1

12.0	12.0	17.0
10.0	17.0	19.0
9.0	6.0	14.0

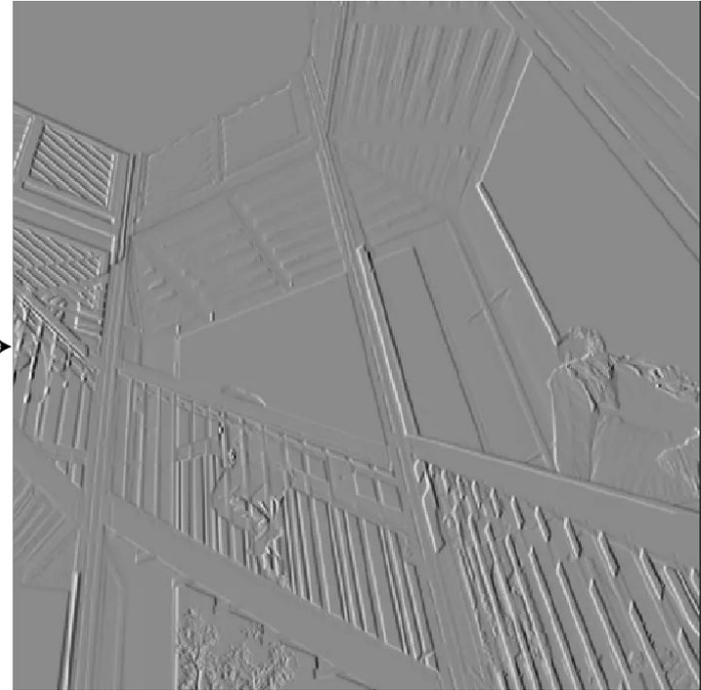


# Filtrado lineal (Bordes = Altas frecuencias)

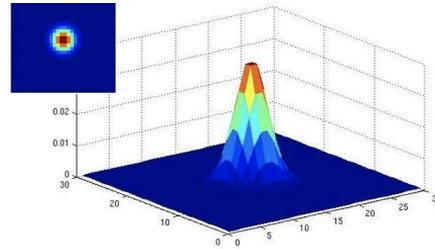


$$\begin{bmatrix} +1 & 0 & -1 \\ +2 & 0 & -2 \\ +1 & 0 & -1 \end{bmatrix}$$

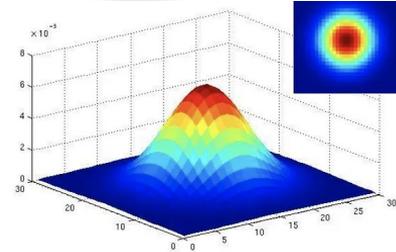
Horizontal Sobel kernel



# Filtro que representa un Lente = Gaussian Kernel



$\sigma = 2$  with  $30 \times 30$   
kernel

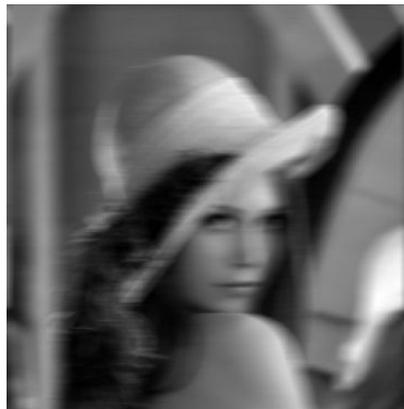


$\sigma = 5$  with  $30 \times 30$   
kernel

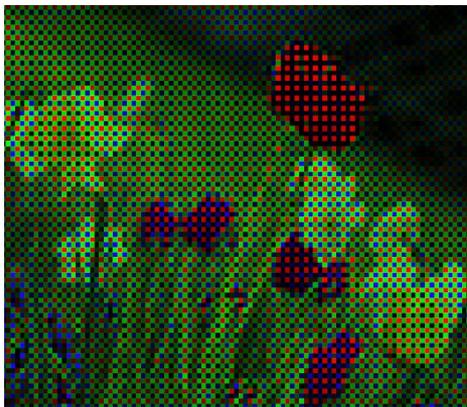
# Problemas a Resolver

1. Demosaicking
2. Deconvolution/Deblurring
3. Denoising

Deconvolution



Demosaicking



Denoising



# Hands-on: Transformaciones y Demosaicing

# Actualicemos el repositorio!

main

1 Branch 0 Tags

Go to file

t

Add file

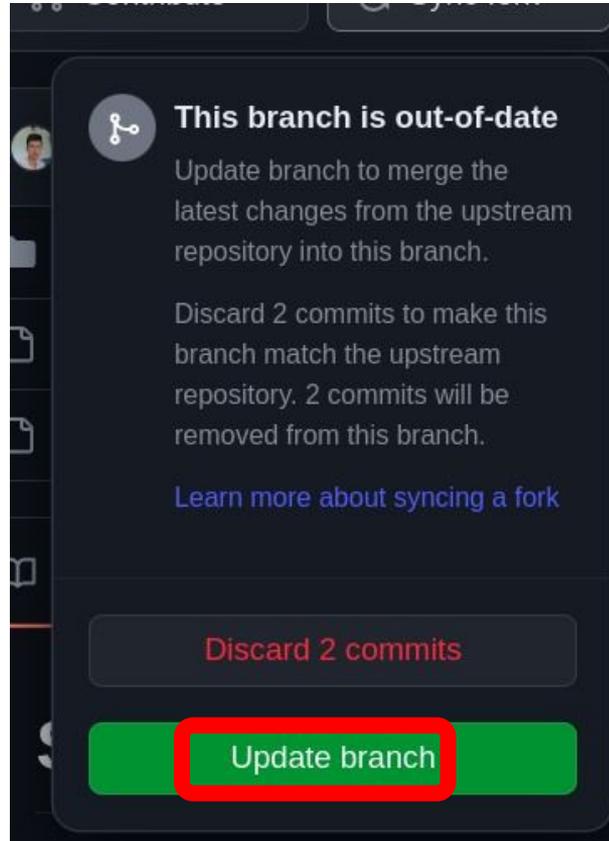
Code

This branch is 2 commits ahead of, 3 commits behind `semilleroCV/Hands-on-Computer-Vision:main`.

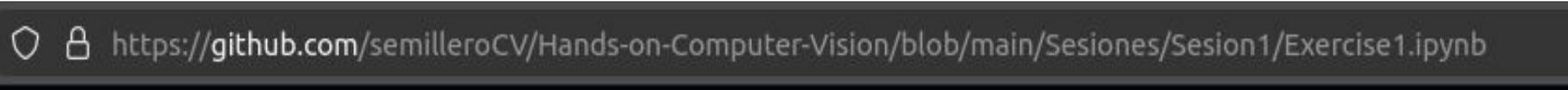
Contribute

Sync fork

# Actualicemos el repositorio!

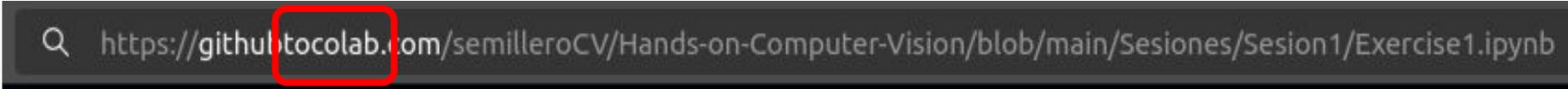


# Abrelo en colab usando “githubtocolab”

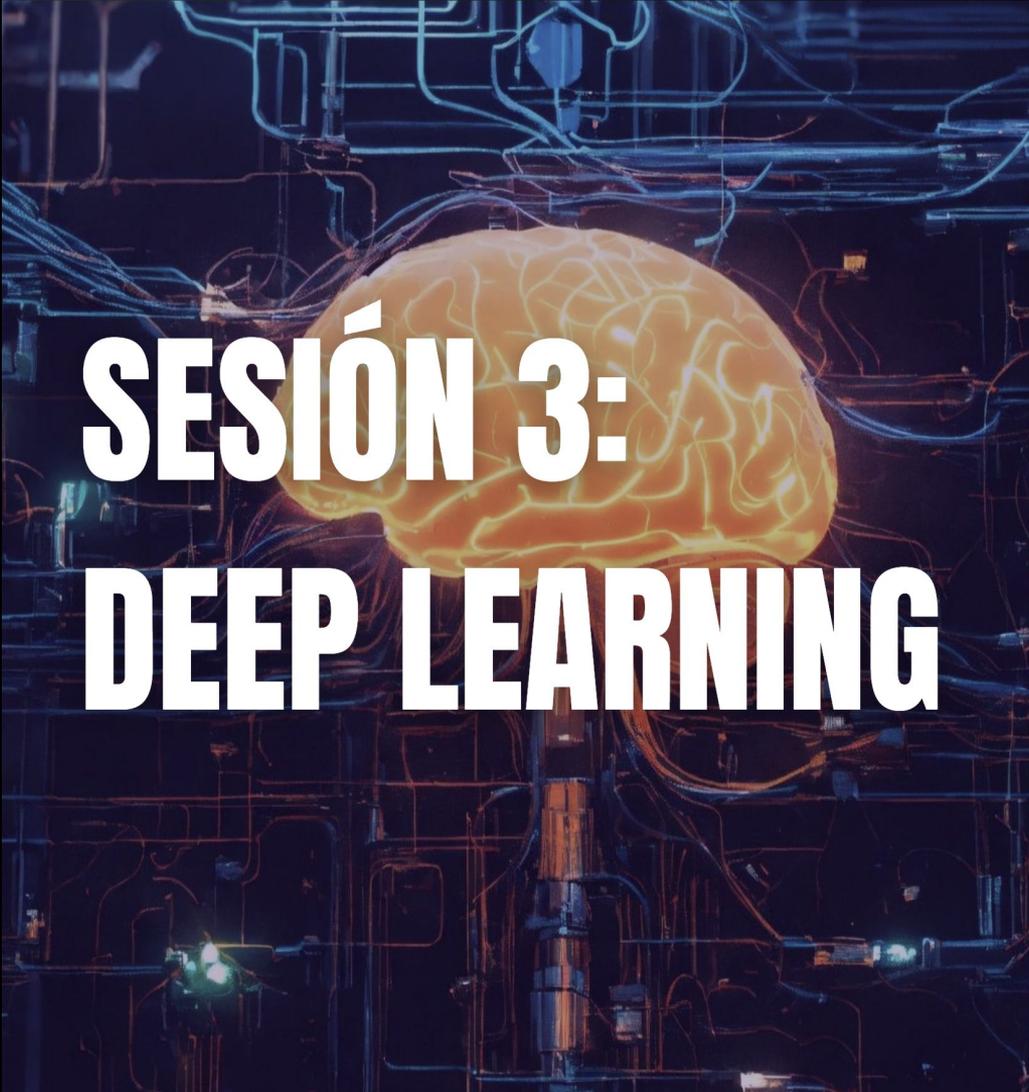
 https://github.com/semilleroCV/Hands-on-Computer-Vision/blob/main/Sesiones/Sesion1/Exercise1.ipynb



Agrega la palabra “tocolab” y da ENTER

 https://github**tocolab**.com/semilleroCV/Hands-on-Computer-Vision/blob/main/Sesiones/Sesion1/Exercise1.ipynb

**Next  
Week**



**SESIÓN 3:  
DEEP LEARNING**